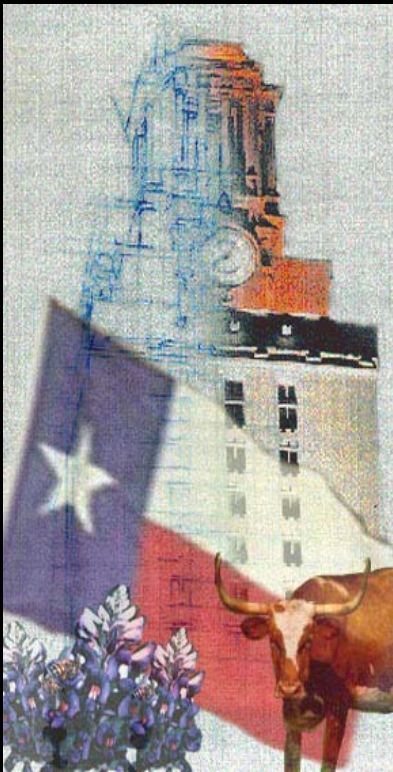


Development of a New Family of Normalized Modulus Reduction and Material Damping Curves



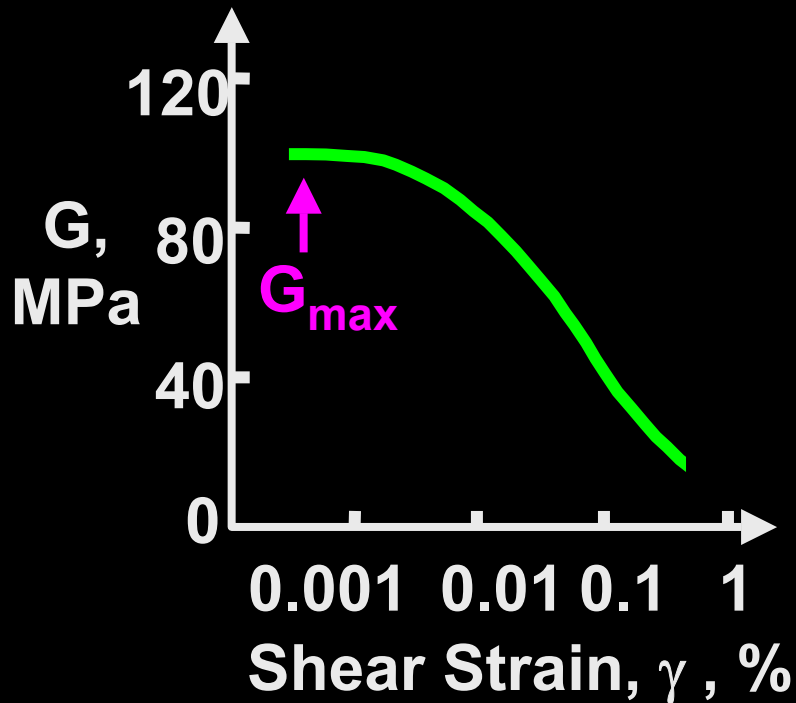
**K.H. Stokoe, II, M.B. Darendeli
F.-Y. Menq, W.K. Choi, and
R.B. Gilbert**

University of Texas at Austin

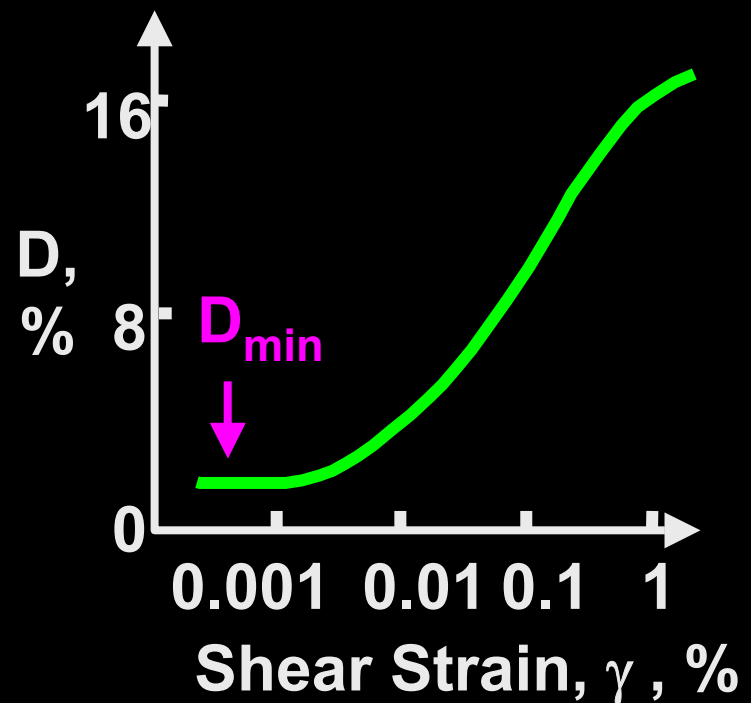
**Int. Workshop on Uncertainties
in Soil Properties and Site
Response
March 2004**

Dynamic Soil Properties

Shear Modulus, G



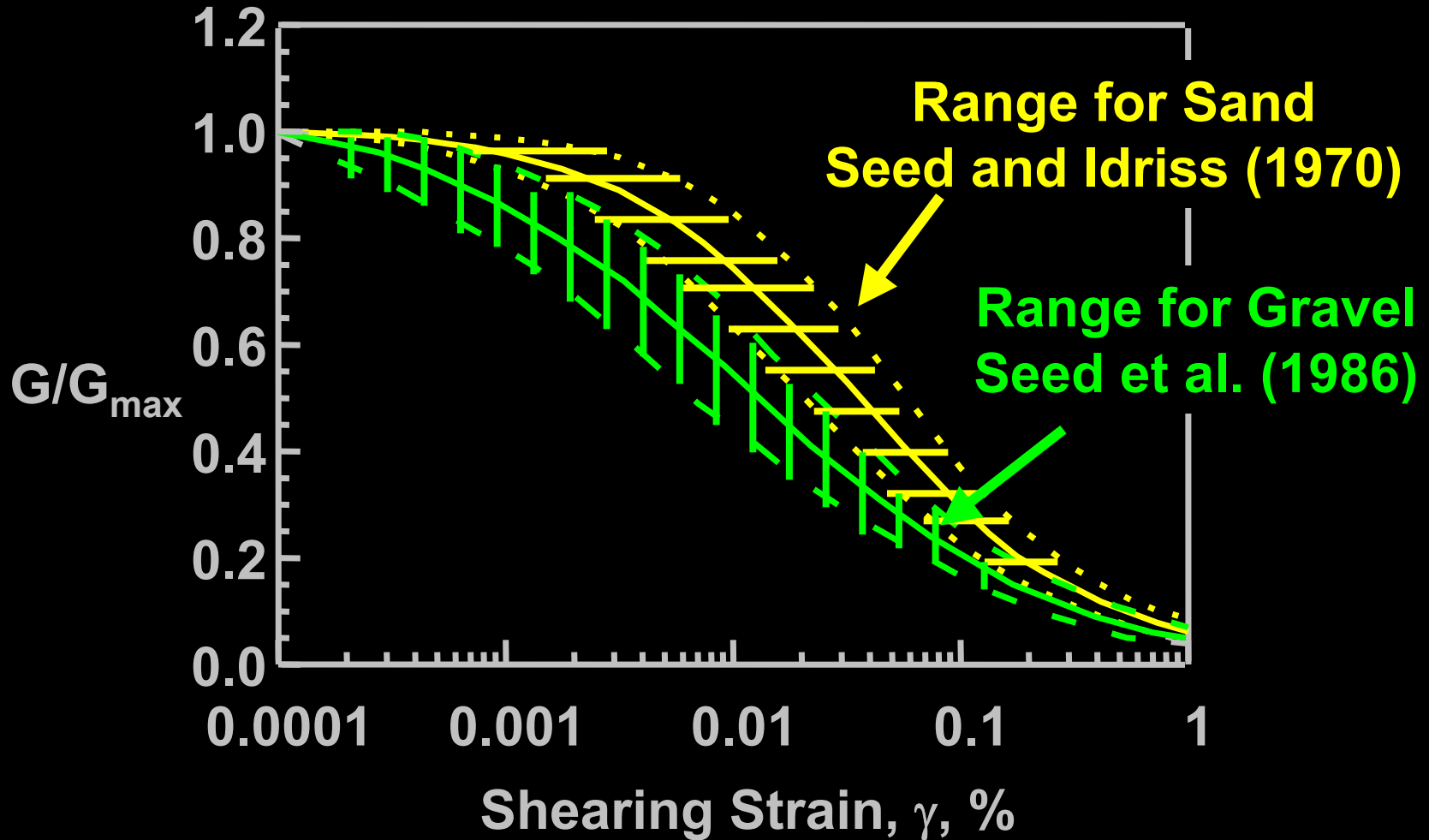
Material Damping Ratio, D



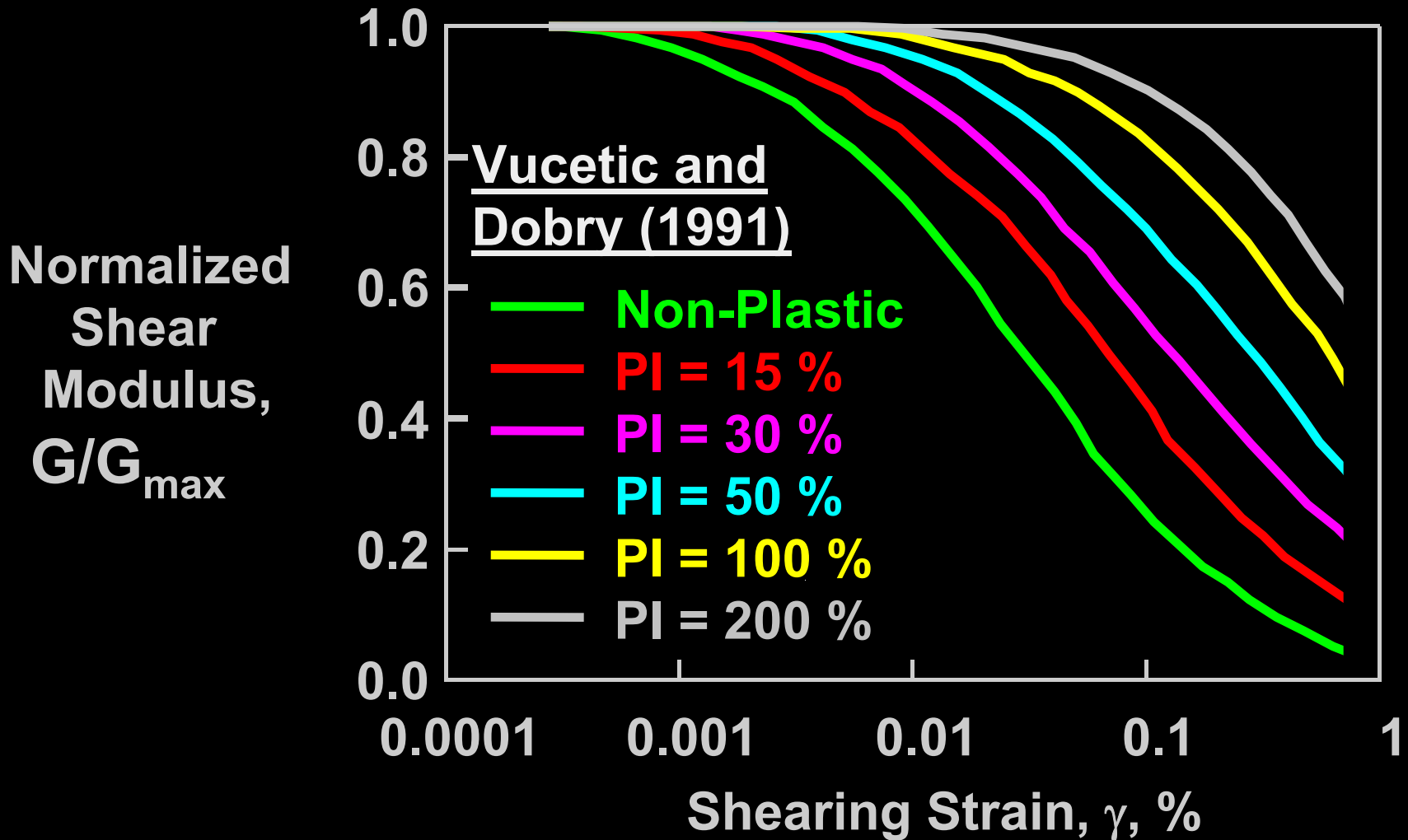
Examples of Empirical Relationships Based on Laboratory Studies

- **Seed et al., 1970**
- **Hardin and Drnevich, 1972**
- **Kokusho, 1980**
- **Seed et al., 1986**
- **Sun et al., 1988**
- **Idriss, 1990**
- **Vucetic and Dobry, 1991**
- **Ishibashi and Zhang, 1993**

Nonlinear Behavior of Sandy and Gravelly Soils



Effect of Soil Plasticity on Nonlinear Behavior (Vucetic and Dobry, 1991)



Objective

To generate a new family of empirical G/G_{\max} – $\log \gamma$ and D – $\log \gamma$ curves such that the observed effects of various parameters on G/G_{\max} and D are represented more accurately:

- **Shearing Strain Amplitude, γ**
- **Soil Type (expressed by PI , C_u , D_{50})**
- **Effective Confinement, σ_o'**
- **Number of Cycles, N**
- **Loading Frequency, f**
- **Overconsolidation Ratio, OCR**

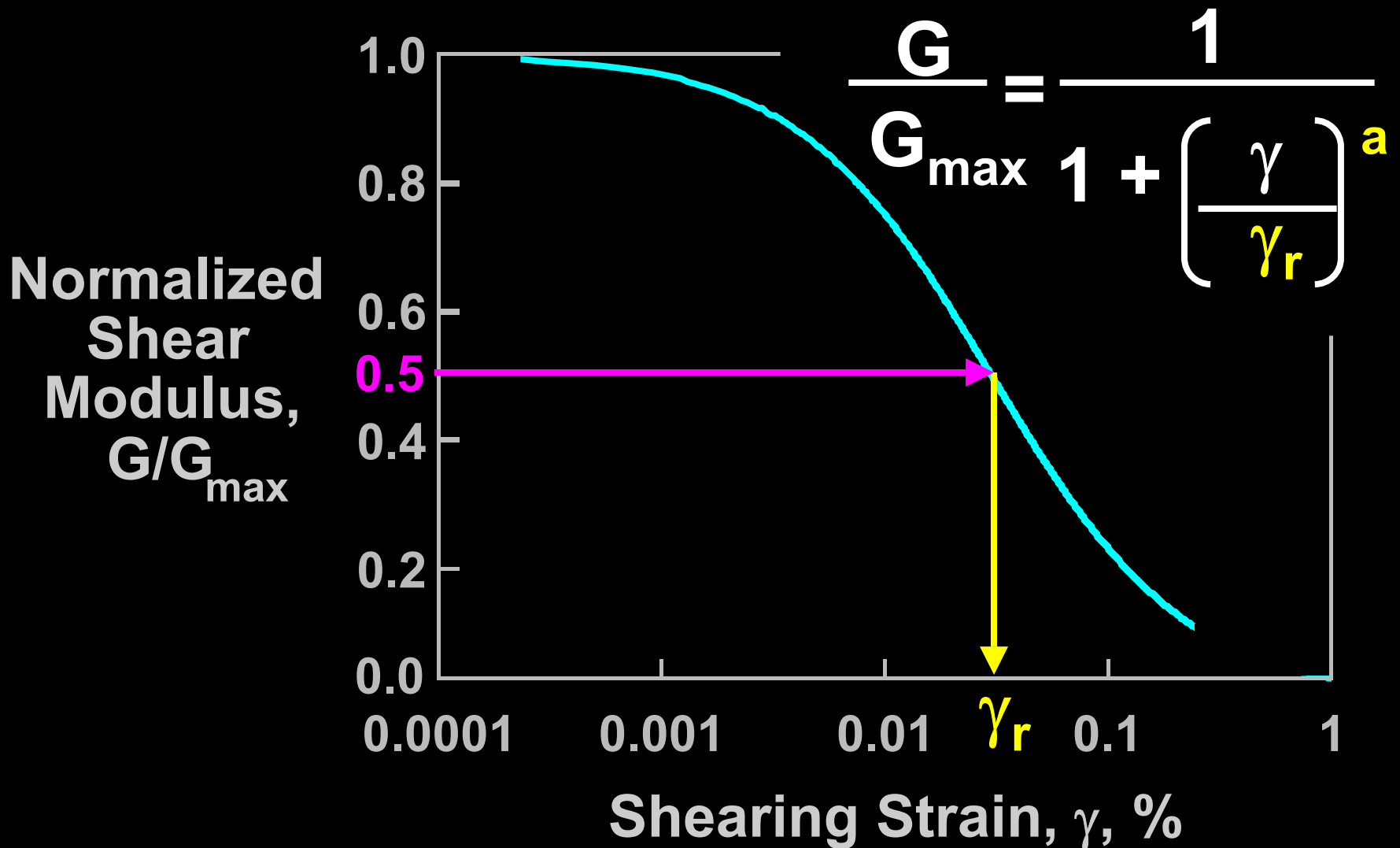
**much like
Hardin
and
Drnevich,
1972**

Proposed 5- Parameter Model (Modified Hyperbolic Model)

$$\frac{G}{G_{\max}} = \frac{1}{1 + \left(\frac{\gamma}{\gamma_r}\right)^a}$$

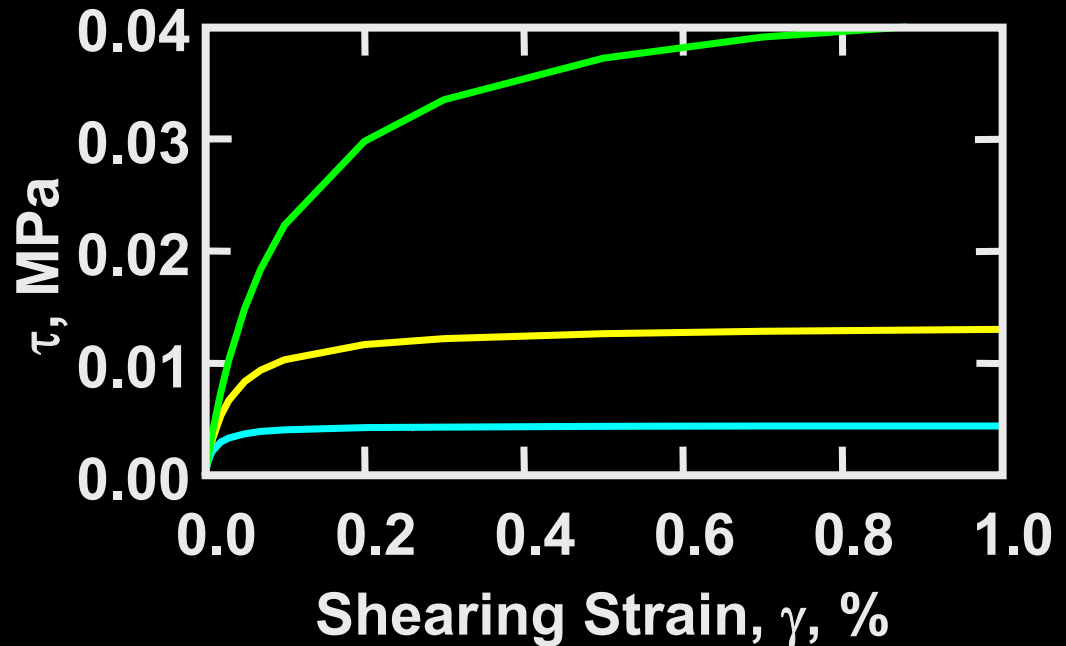
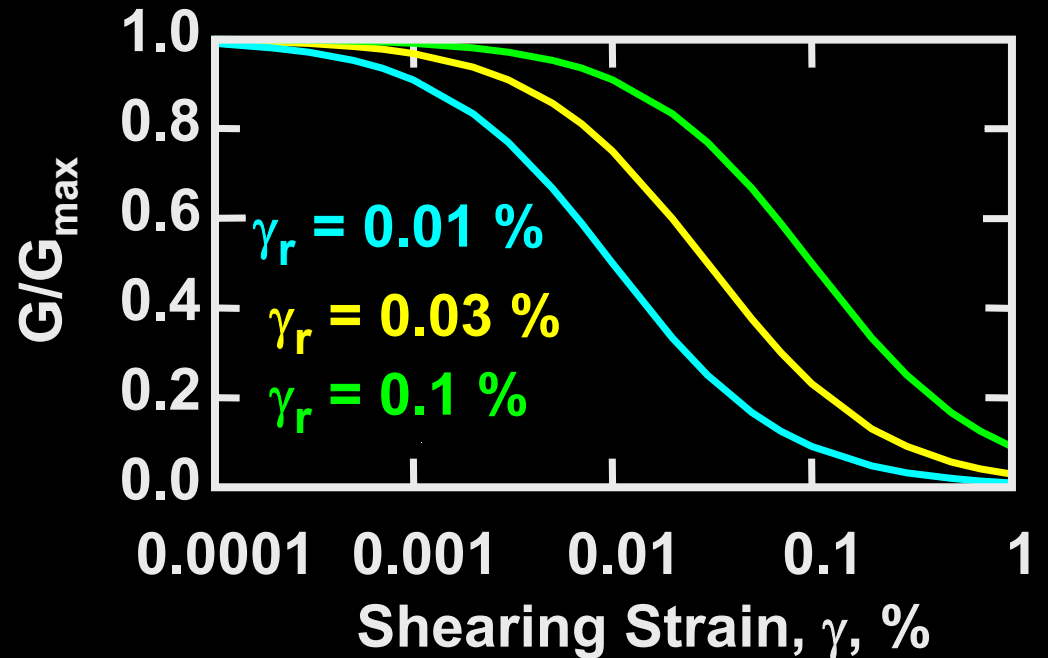
$$D = D_{\min} + D_{\text{Masing}} * \left(b * \left(\frac{G}{G_{\max}} \right)^c \right)$$

Proposed Model: $G/G_{\max} - \log \gamma$

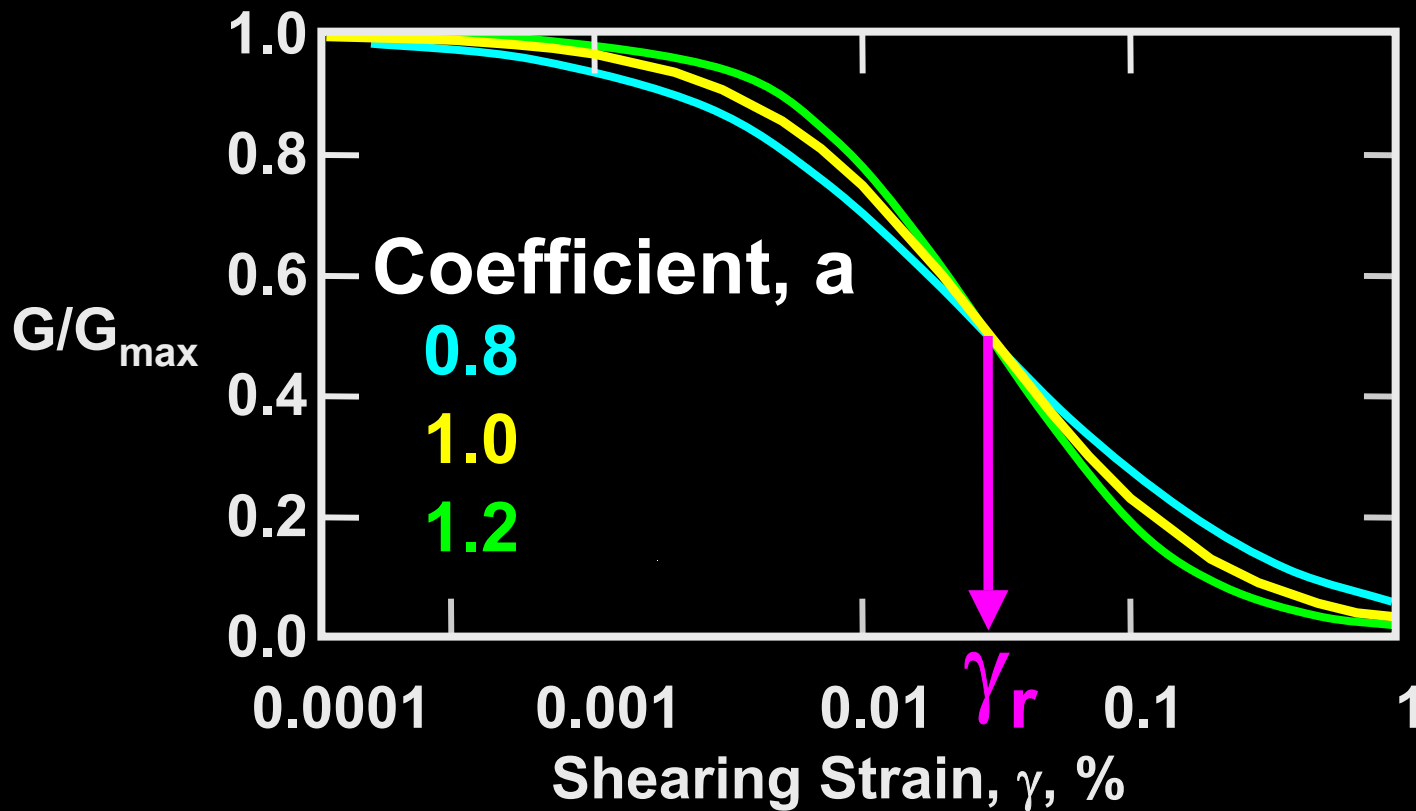


Effect of Reference Strain, γ_r , on:

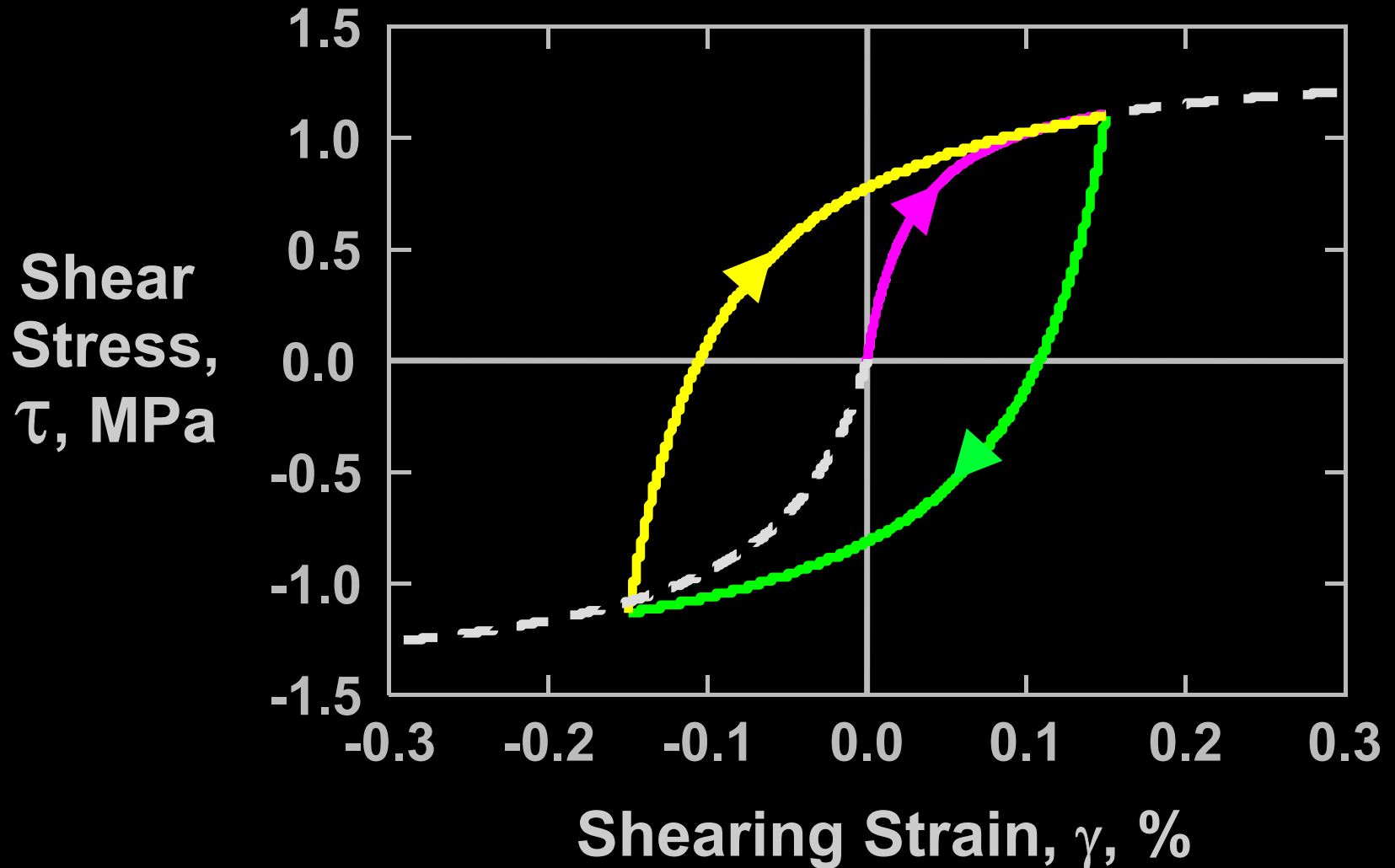
1. $G/G_{\max} - \log \gamma$
2. $\tau - \log \gamma$
($a = 1$)



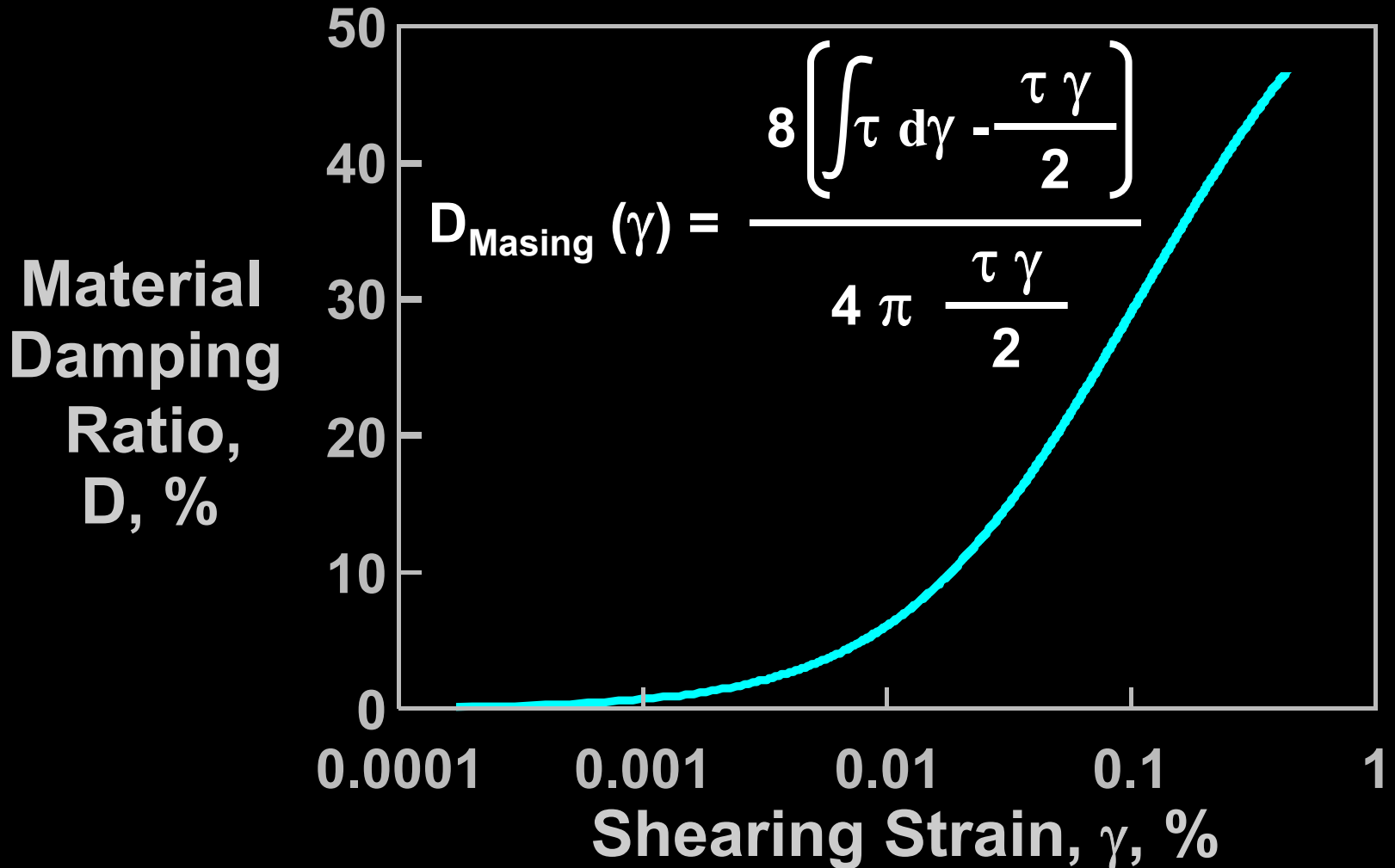
Effect of Coefficient “a” on G/G_{\max} – $\log \gamma$ Curves



Masing (1926) Behavior

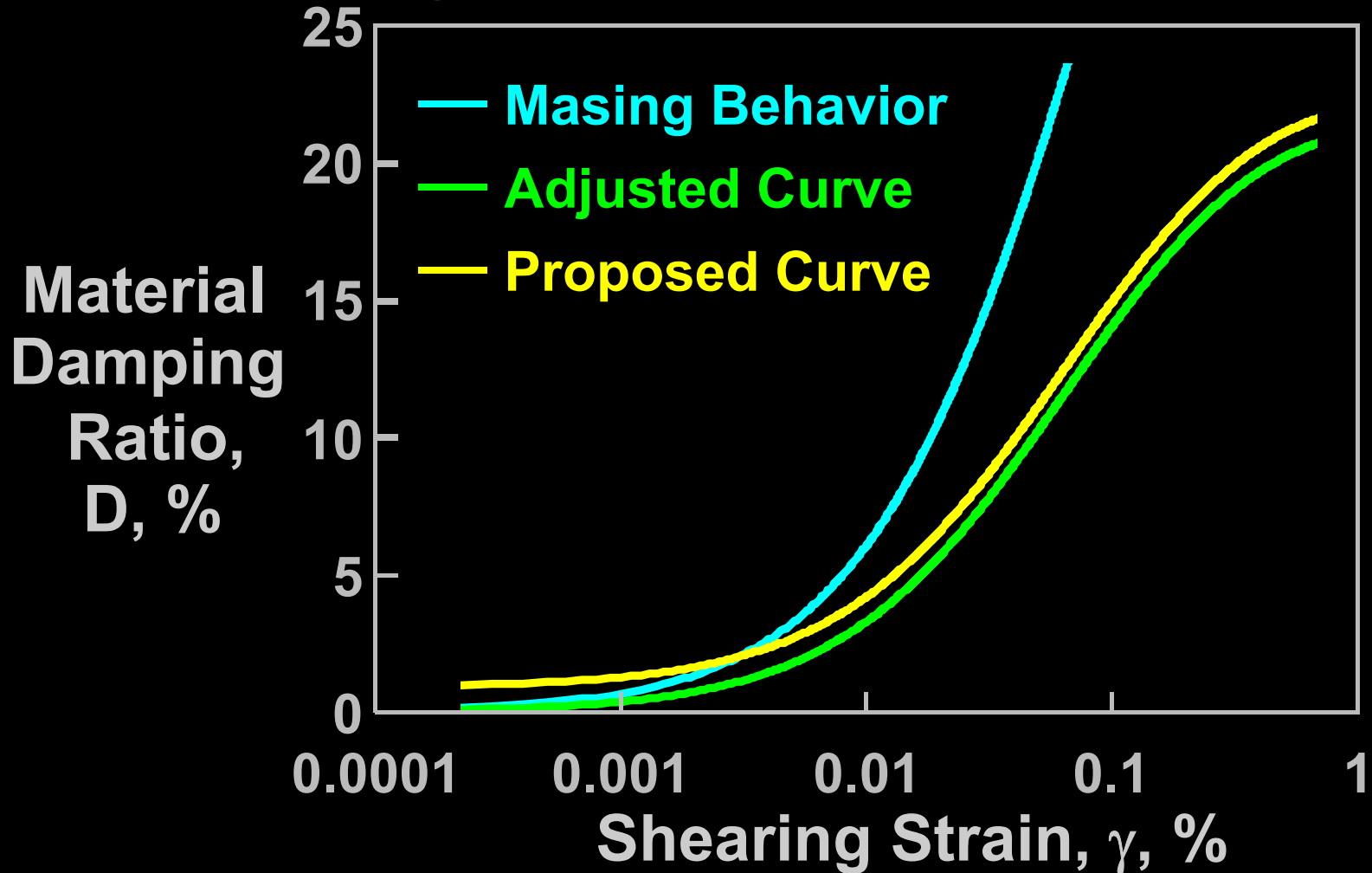


Masing Behavior: $D - \log \gamma$

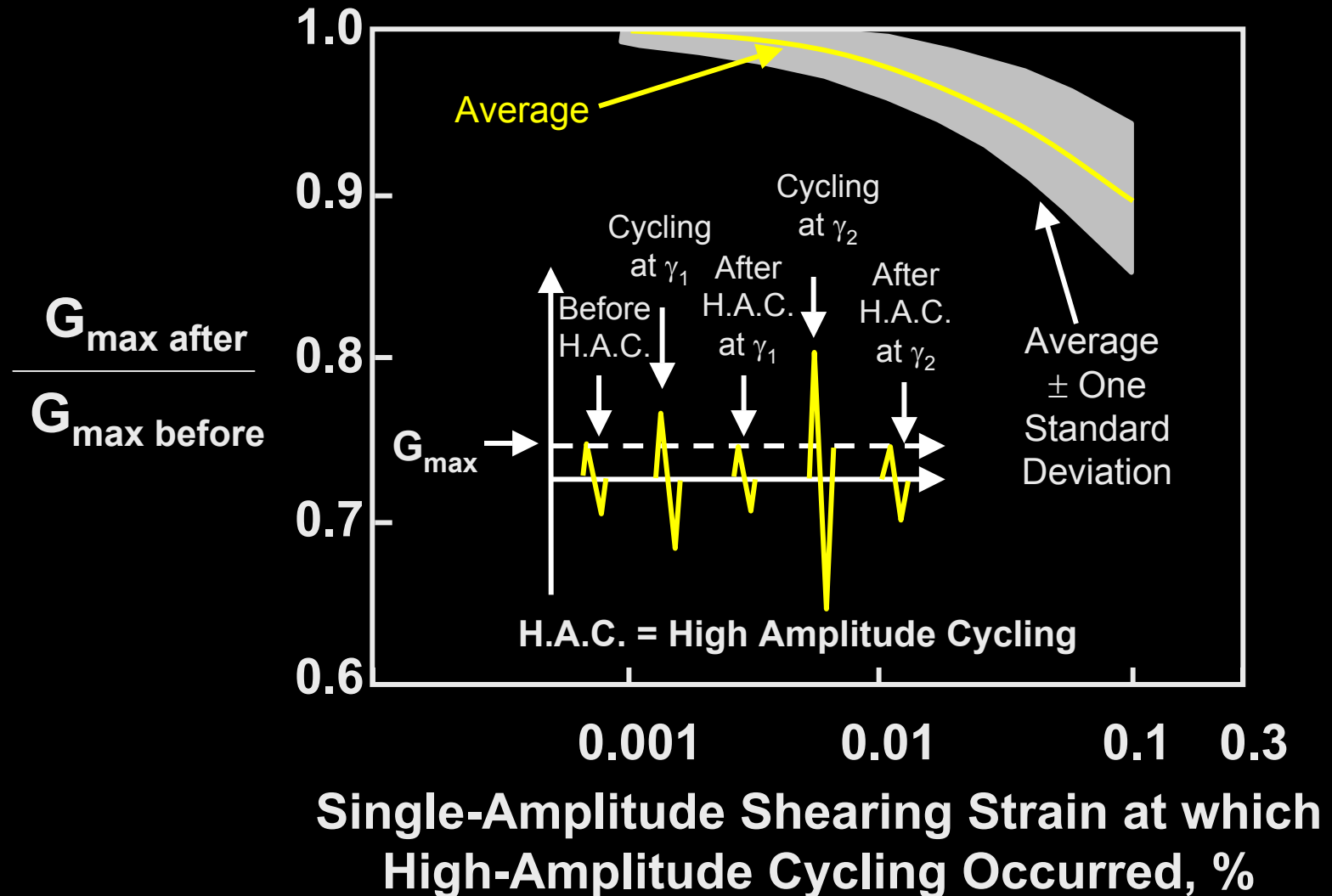


Proposed Model: $D - \log \gamma$

$$D = D_{\text{Masing}} * [b * (G/G_{\text{max}})^c] + D_{\text{min}}$$



G_{\max} Degradation with γ : “c” Parameter



Relationships Between Five Parameters and Soil Type and Loading Conditions: Plastic Soils

- $\gamma_r = f (PI, OCR, \sigma_0')$
- $a = \text{constant} = 0.92$
- $D_{\min} = f (PI, OCR, \sigma_0', f)$
- $b = f (N)$
- $c = \text{constant} = 0.10$

Bayesian Approach

Bayesian Approach is a systematic way of combining information based on experience (or intuition) with observational data.

- **The problem is structured analytically.**
- **Unknown parameters are modeled as random variables.**
- **Expected values based on experience and confidence intervals associated with these estimates are determined.**
- **These values are updated such that the likelihood of occurrence of the observational data is maximized.**

Recommended Values: Plastic Soils

$$\gamma_r = (\phi_1 + \phi_2 * PI * OCR^{\phi_3}) * \sigma_o'^{\phi_4}$$
$$a = \phi_5$$

where: σ_o' = mean effective confining pressure (atm),

PI = soil plasticity (%),

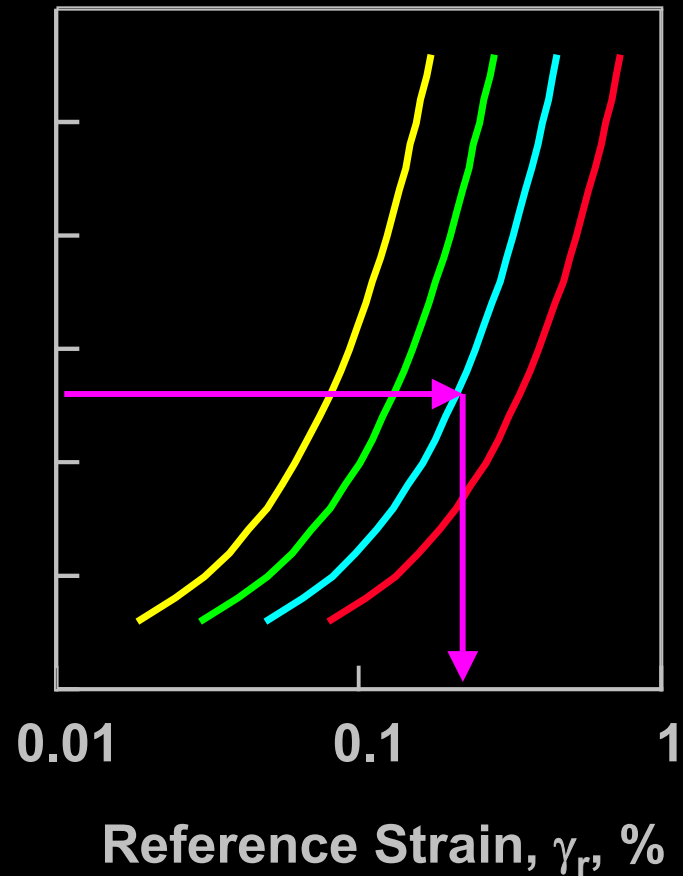
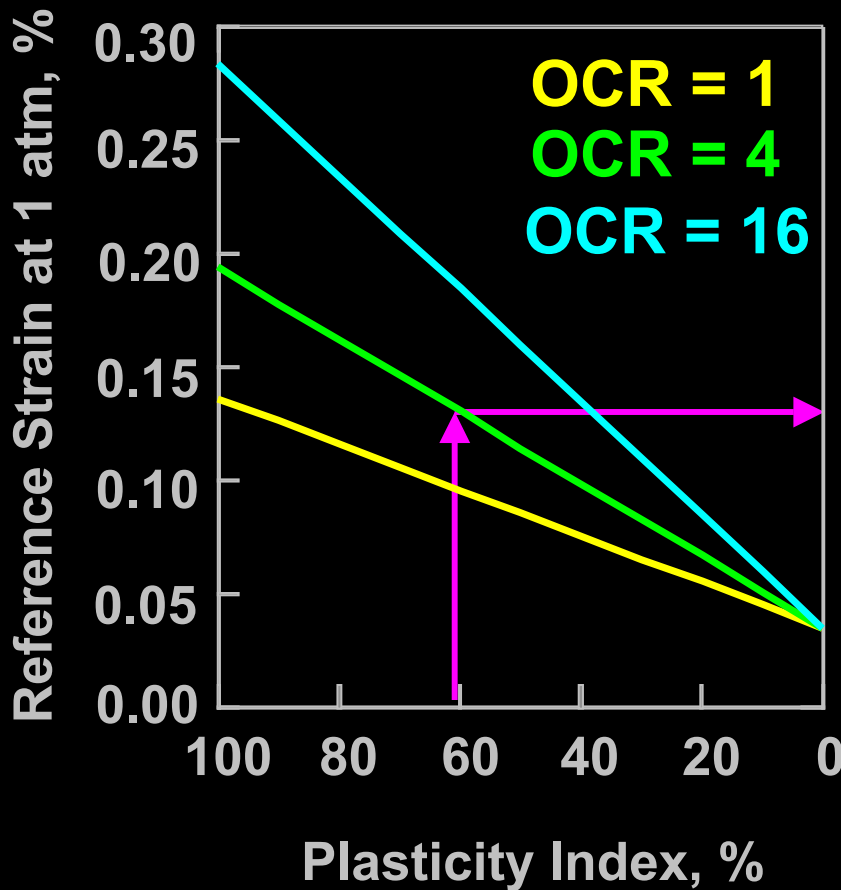
OCR = overconsolidation ratio,

and

$$\phi_1 = 0.0352, \quad \phi_2 = 0.0010, \quad \phi_3 = 0.3246,$$
$$\phi_4 = 0.3483, \quad \phi_5 = 0.9190$$

Results: γ_r for PI = 60%,
 OCR = 4
 and $\sigma'_o = 4$ atm

$\sigma'_o = 0.25$ atm
 $\sigma'_o = 1$ atm
 $\sigma'_o = 4$ atm
 $\sigma'_o = 16$ atm



Recommended Values: Plastic Soils

$$D_{\min} = (\phi_6 + \phi_7 * PI * OCR^{\phi_8}) * \sigma_o'^{\phi_9} * [1 + \phi_{10} * \ln(f)]$$

$$b = \phi_{11} + \phi_{12} * \ln(N)$$

where: σ_o' = mean effective confining pressure (atm),

PI = soil plasticity (%),

OCR = overconsolidation ratio,

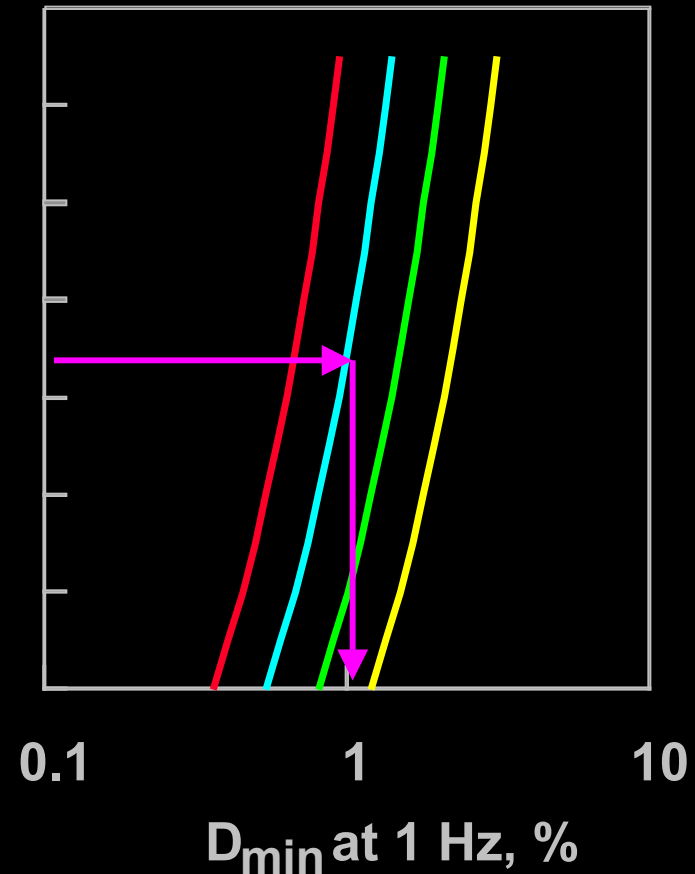
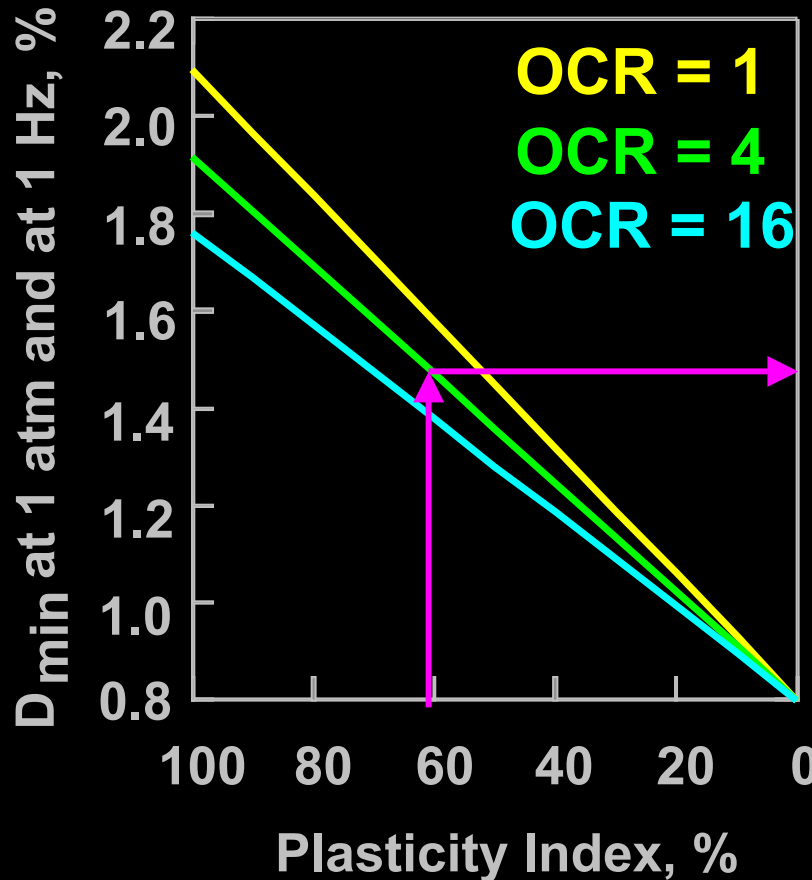
f = loading frequency,

N = number of loading cycles,

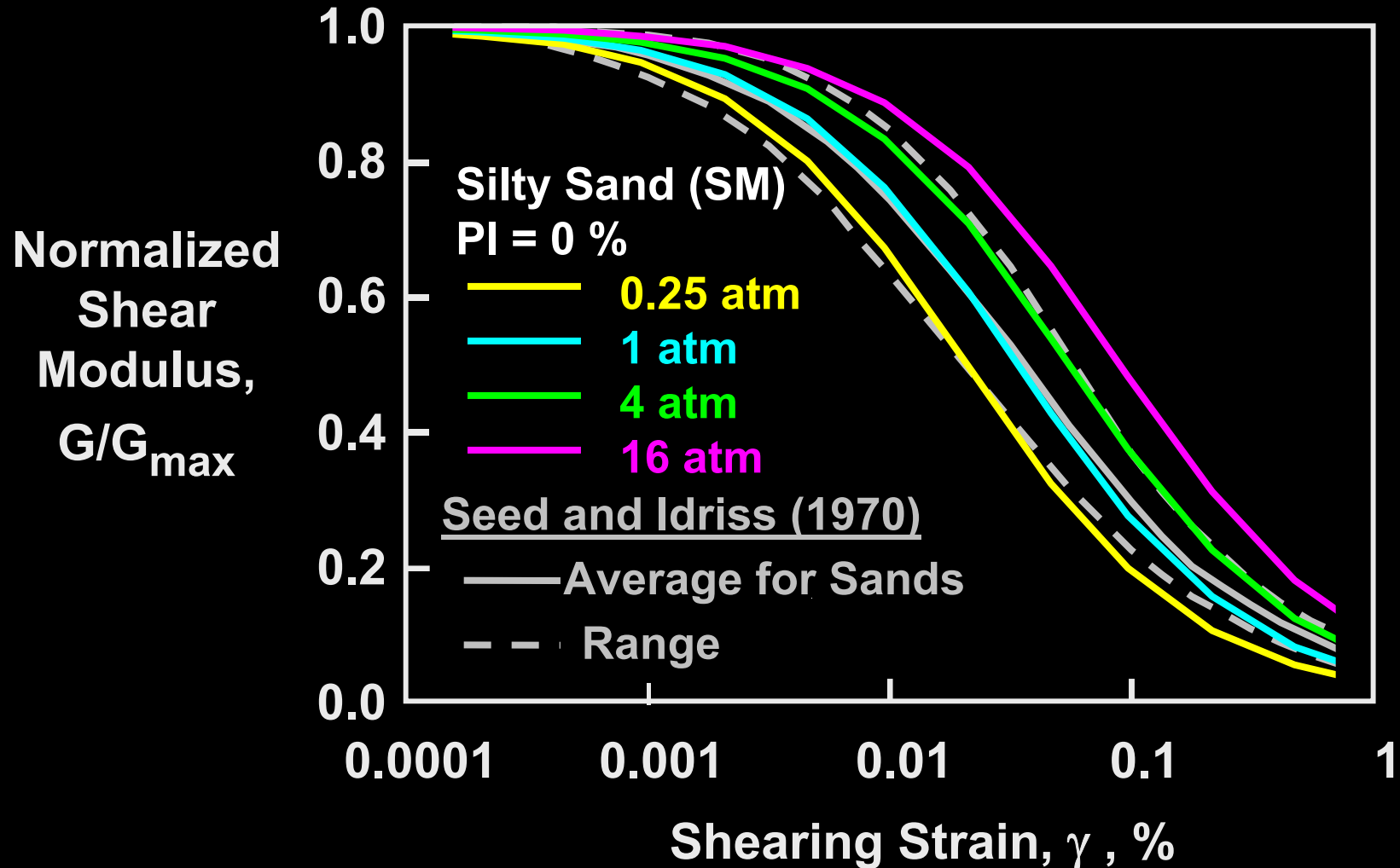
**and $\phi_6 = 0.8005$, $\phi_7 = 0.0129$, $\phi_8 = -0.1069$,
 $\phi_9 = -0.2889$, $\phi_{10} = 0.2919$, $\phi_{11} = 0.6329$,
 $\phi_{12} = -0.0057$**

Results: D_{\min} for PI = 60%,
 OCR = 4
 and $\sigma'_o = 4$ atm

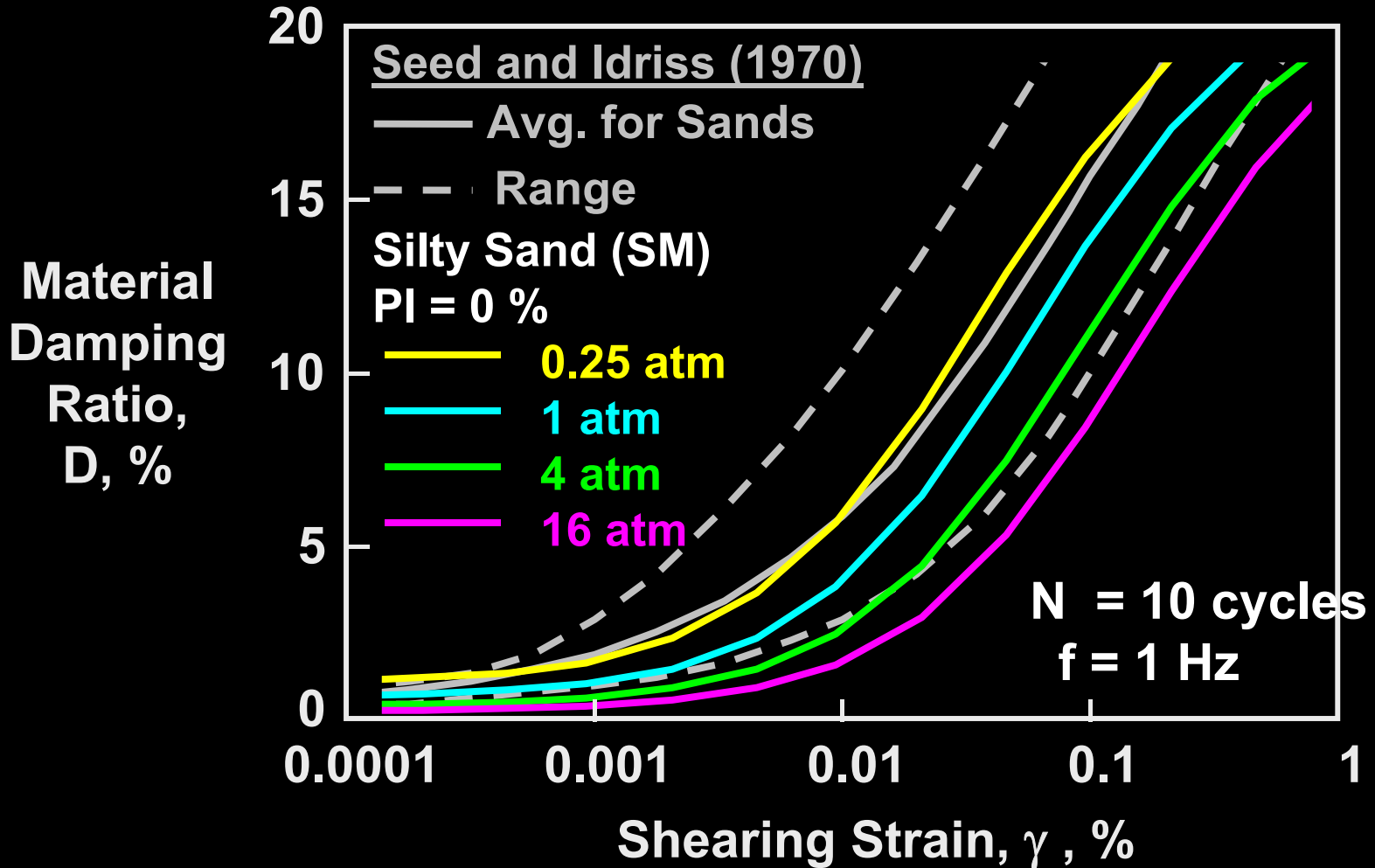
$\sigma'_o = 16$ atm
 $\sigma'_o = 4$ atm
 $\sigma'_o = 1$ atm
 $\sigma'_o = 0.25$ atm



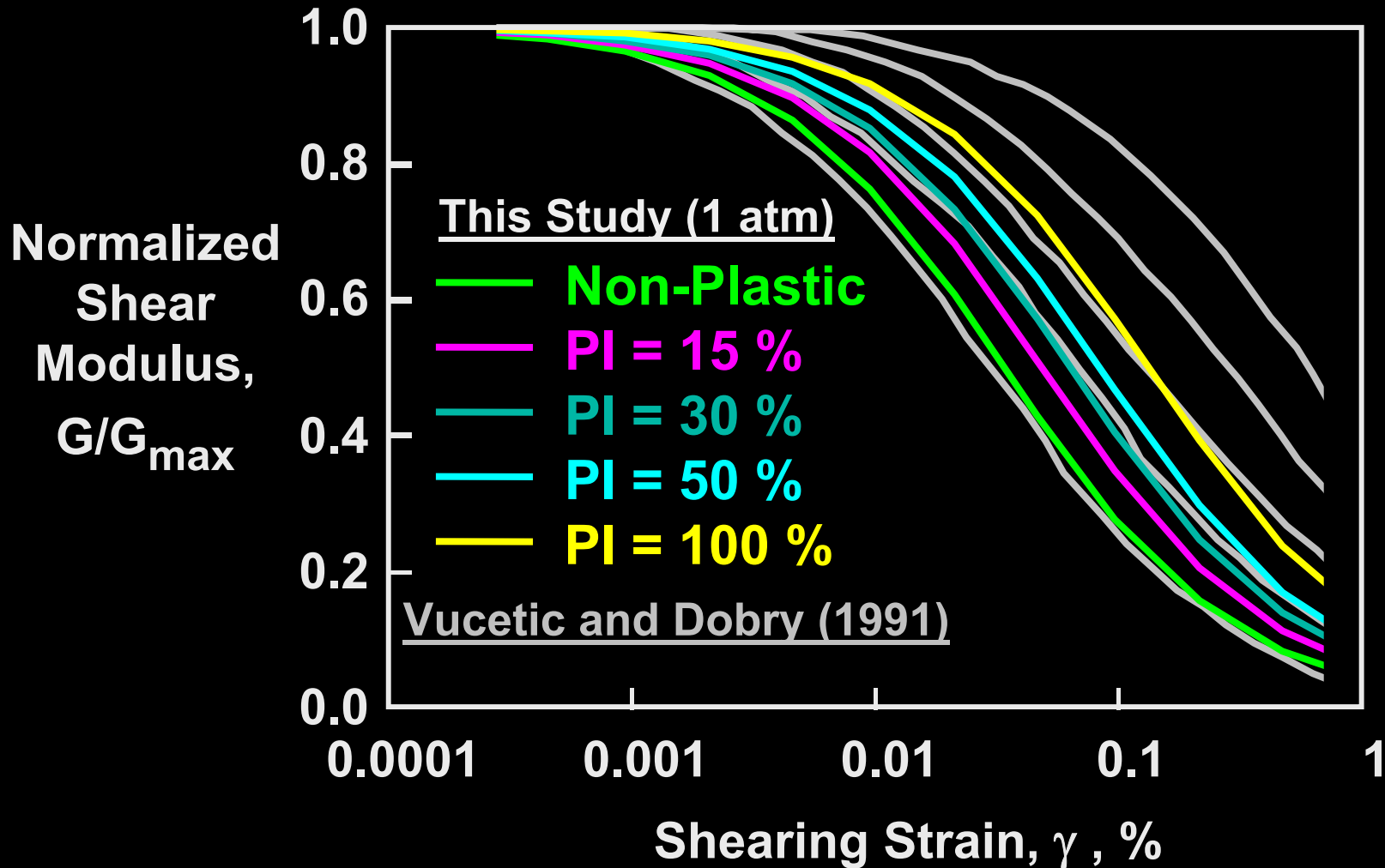
Effect of σ'_o on the Nonlinear Behavior of Sands



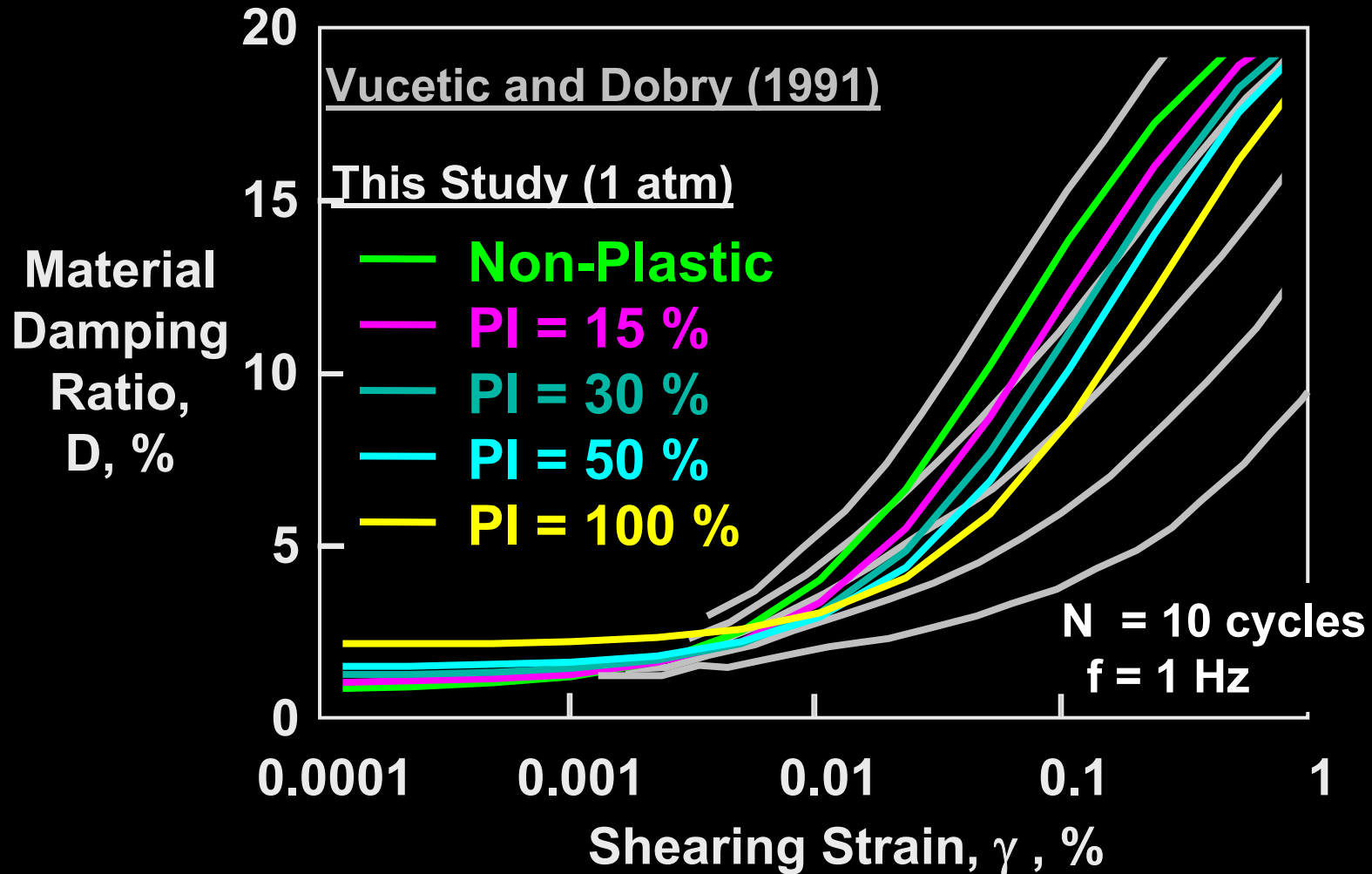
Effect of σ'_o on the Nonlinear Behavior of Sands



Effect of Plasticity on Nonlinear Soil Behavior



Effect of Plasticity on Nonlinear Soil Behavior



Standard Deviations for $G/G_{\max} - \log \gamma$

$$\sigma_{\text{NG}} = \exp(\phi_{13}) + \sqrt{\frac{0.25}{\exp(\phi_{14})} - \frac{(G/G_{\max} - 0.5)^2}{\exp(\phi_{14})}}$$

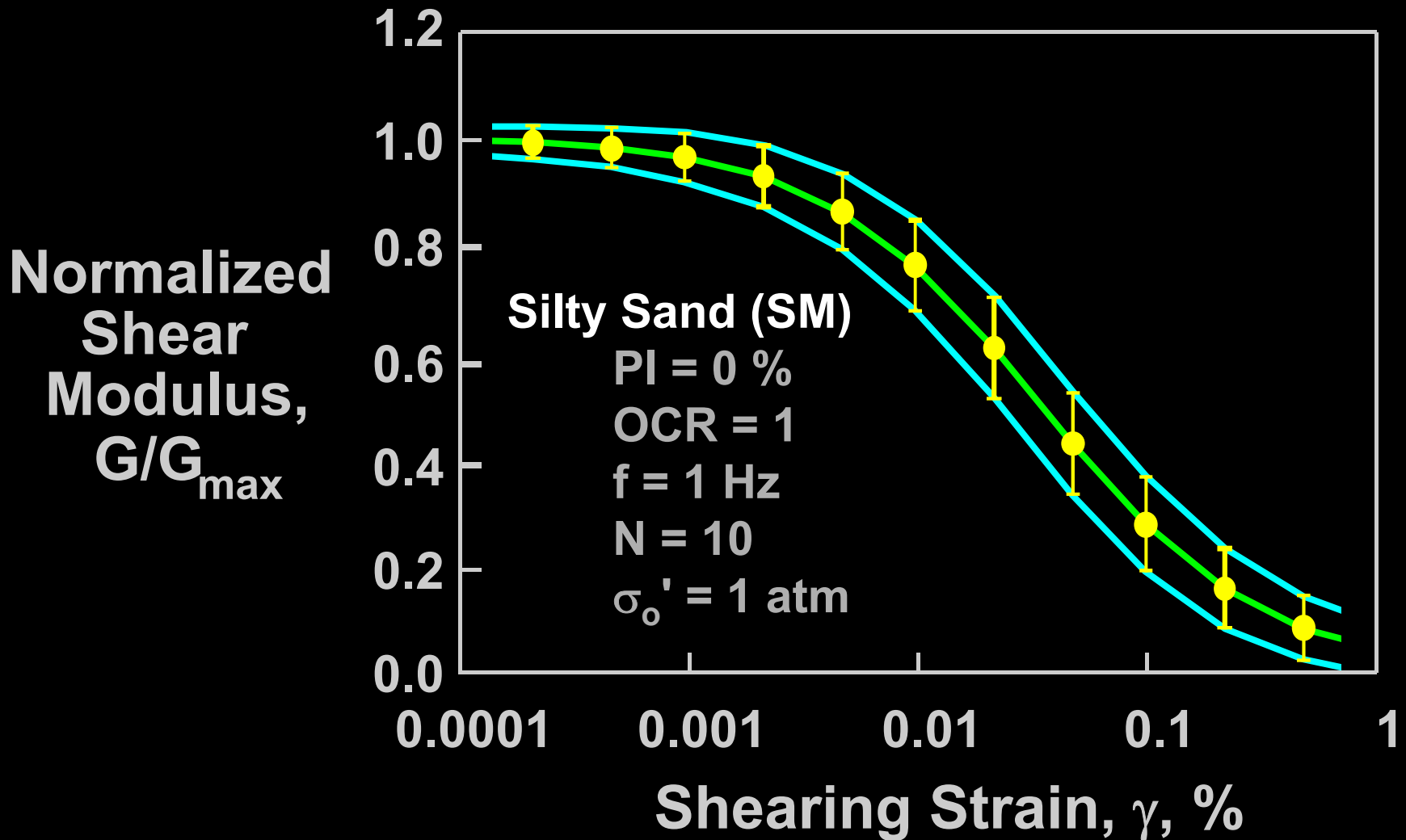
where:

σ_{NG} = standard deviation for normalized modulus reduction curve

G/G_{\max} = estimated normalized shear modulus, and

ϕ_{13} and ϕ_{14} = parameters that relate standard deviation to mean estimate of normalized shear modulus

Uncertainty Associated with the Predicted $G/G_{\max} - \log \gamma$ Curves



Standard Deviations for $D - \log \gamma$

$$\sigma_D = \exp(\phi_{15}) + \exp(\phi_{16}) * \sqrt{D}$$

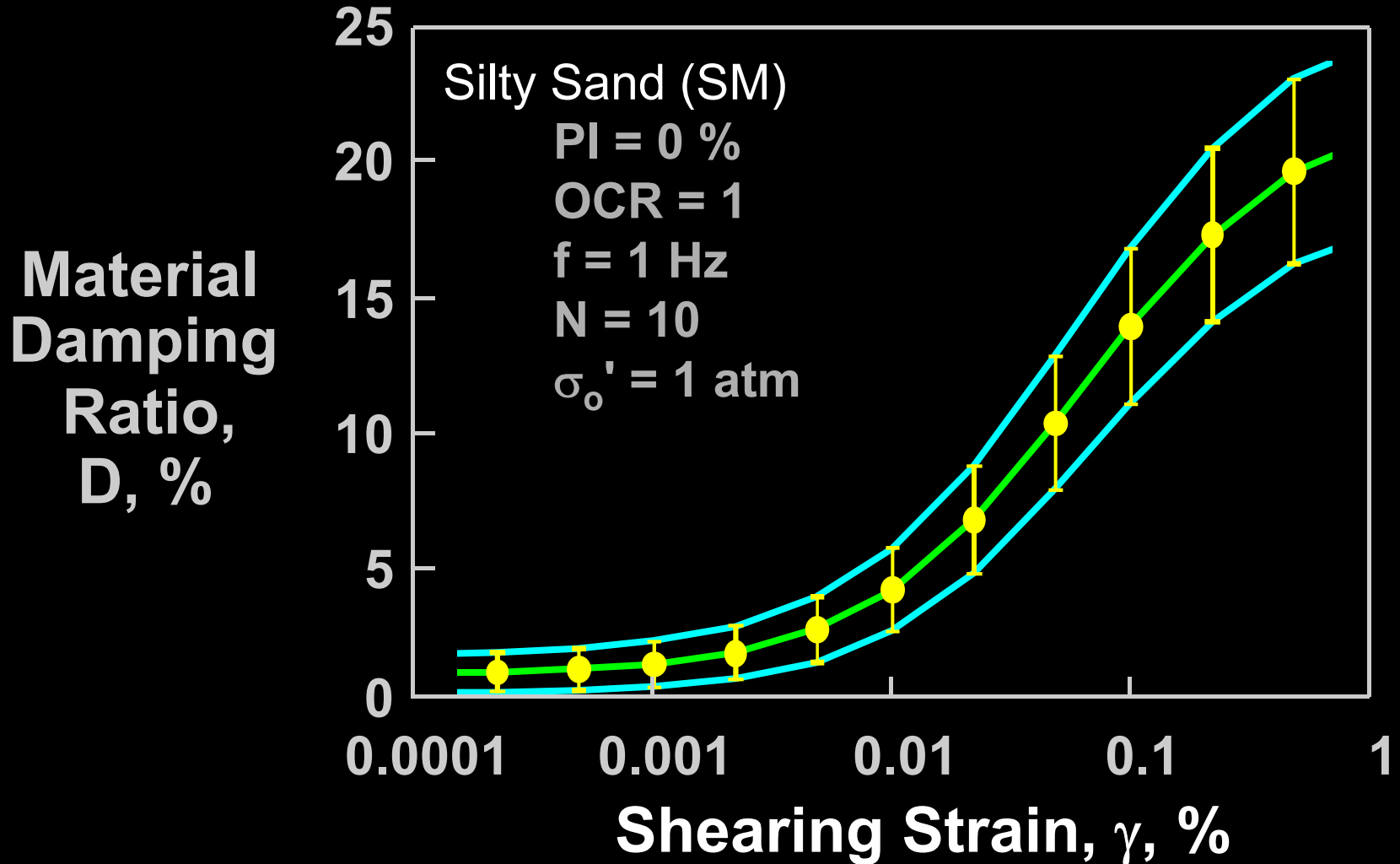
where:

σ_D = standard deviation for material damping curve,

D = estimated material damping ratio, and

ϕ_{15} and ϕ_{16} = parameters that relate standard deviation to the mean estimate of material damping ratio

Uncertainty Associated with the Predicted $D - \log \gamma$ Curves

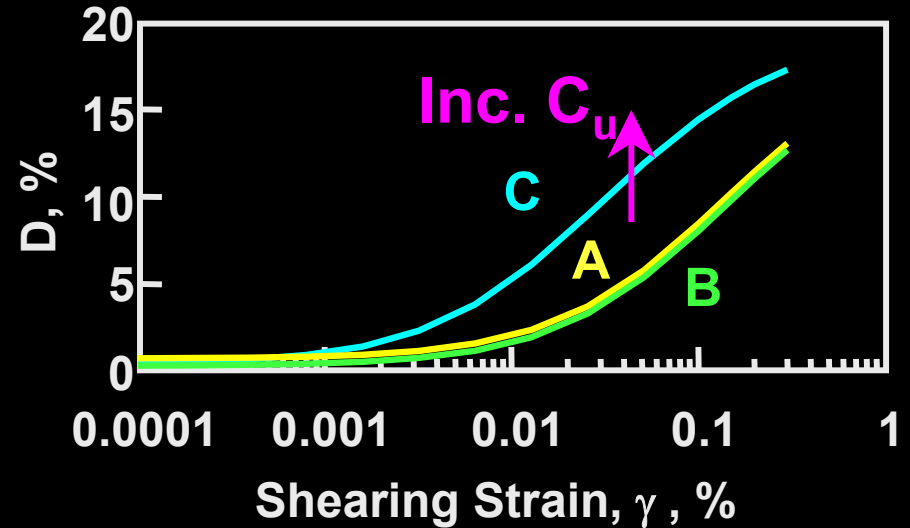
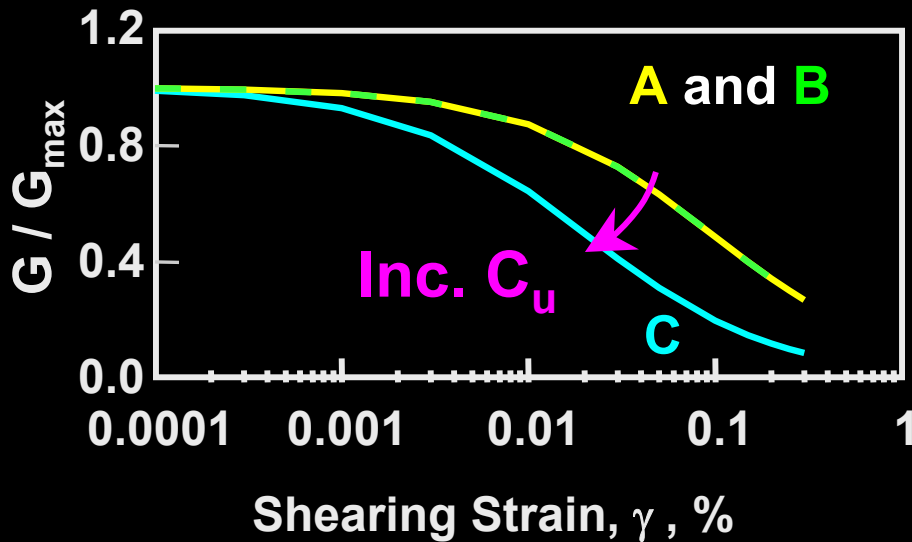
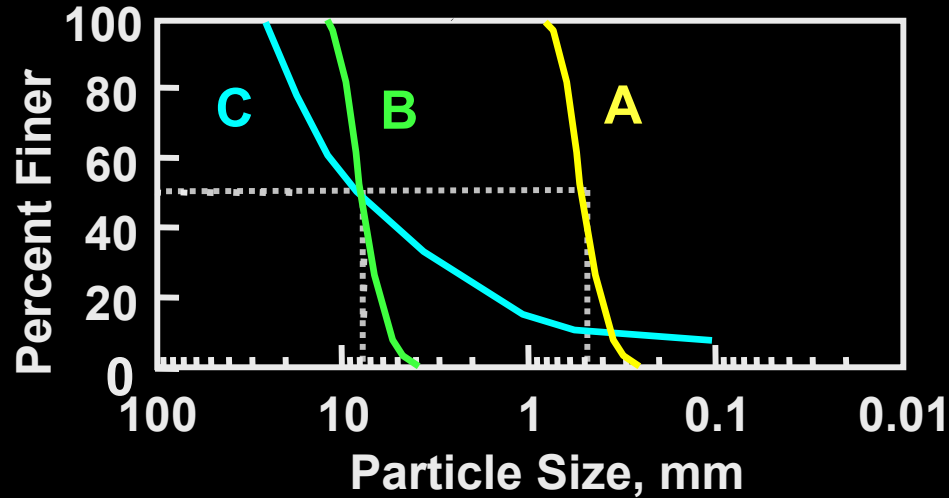


Accomplishments

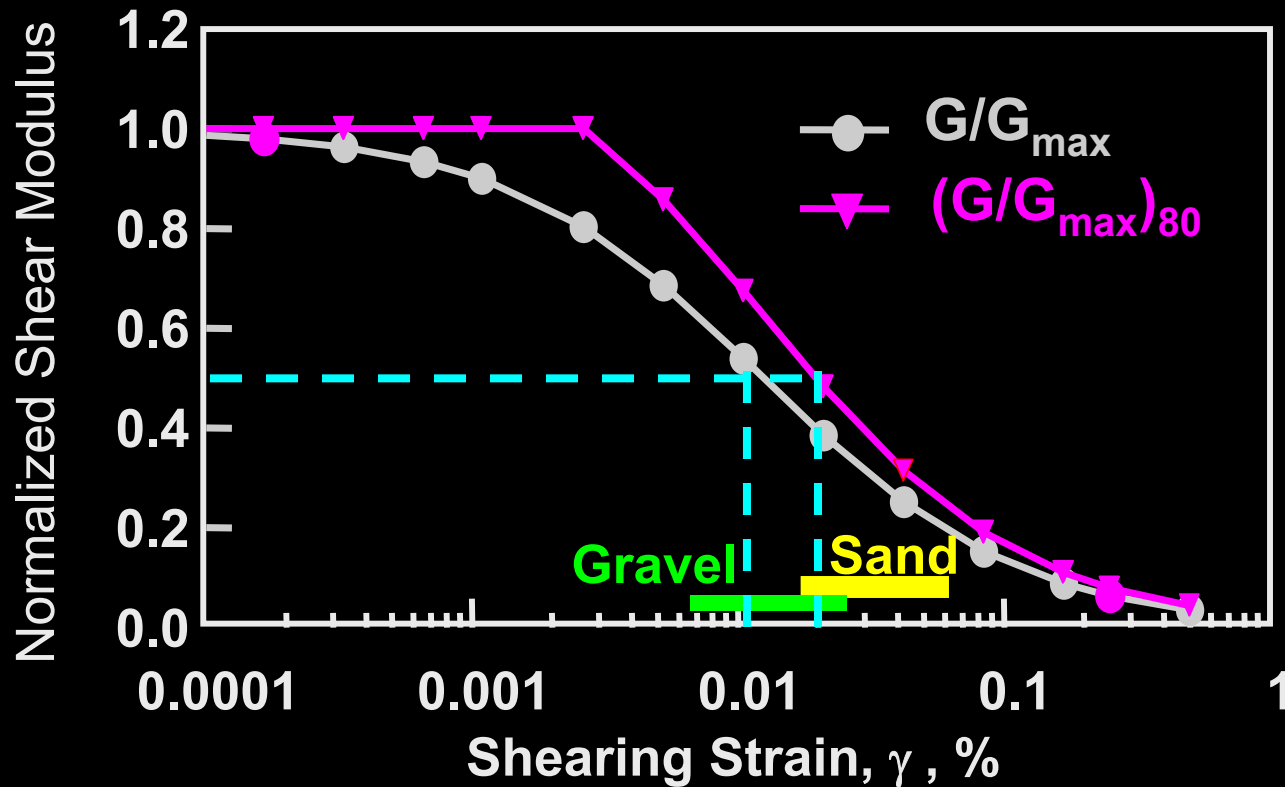
- An empirical formulation to estimate $G/G_{\max} - \log \gamma$ and $D - \log \gamma$ curves for different soils under various loading conditions was generated.
- This formulation was calibrated using data collected at UT over the past decade (with significant input from ROSRINE/PEER).
- $G/G_{\max} - \log \gamma$ and $D - \log \gamma$ curves predicted using the formulation were observed to be consistent with the general trends reported in the literature and observed during the course of this study.
- The uncertainties associated with the predicted curves were also evaluated within the formulation.

Comparison Between SP, GP, and GW

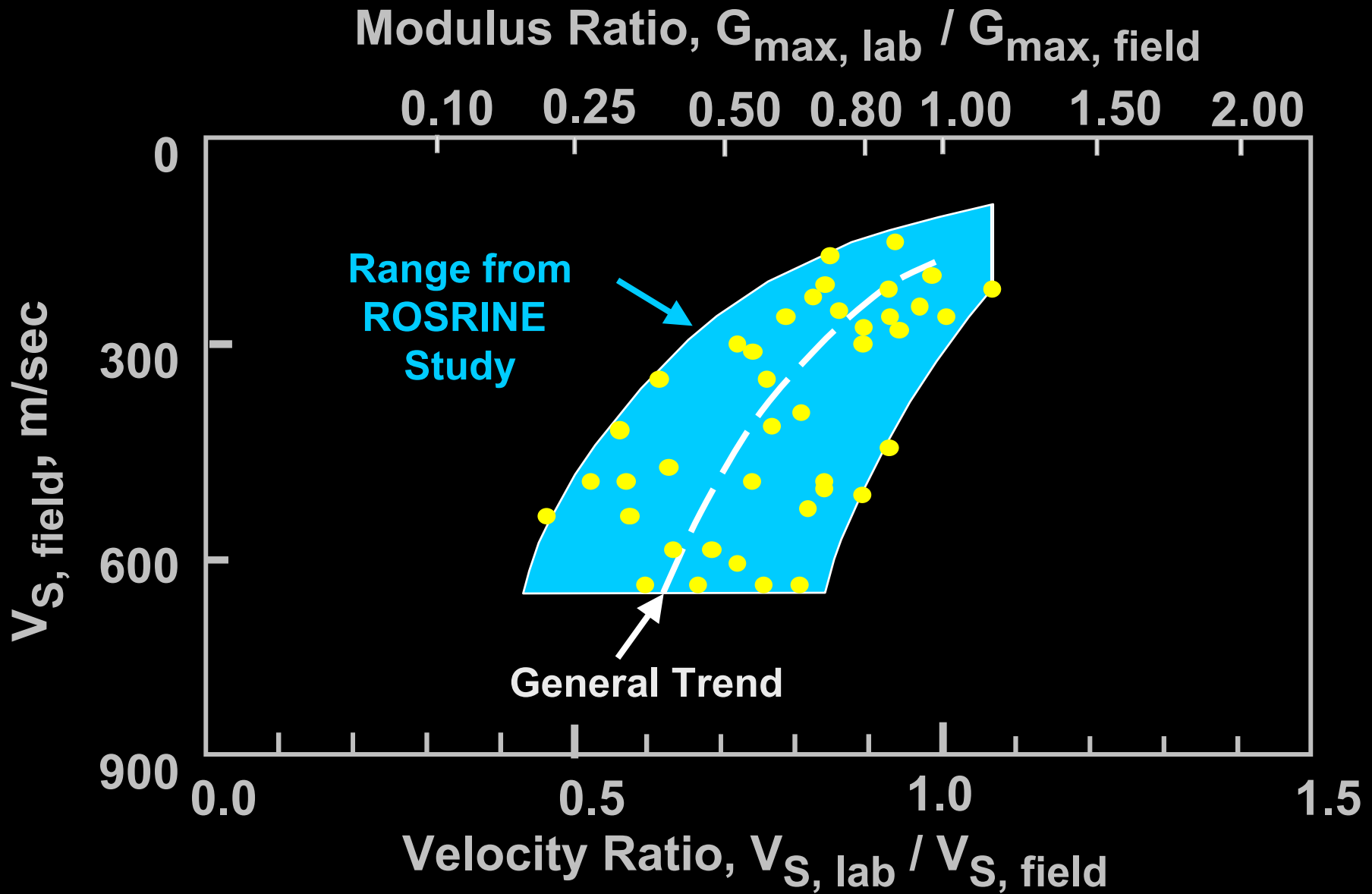
C = Well Graded Gravel (GW)



Problem with Using the Wrong G_{\max}



Effect of Sampling on V_S Values



Thank You

- **Don Anderson, CH2MHill**
- **I.M. Idriss, UC-Davis**
- **Richard Lee, Savannah River**
- **Robert Pyke, Consultant**
- **Cliff Roblee, Caltrans**
- **John Schneider, EPRI**
- **Walt Silva, Pacific Engineering**