

Finite Element Simulation of Earthquake Ground Motion with Coupling Tsunamis in Large Domains

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Objectives

- ◆ **Improve the capabilities of Hercules**—the Quake-group parallel octree-based finite element software package for wave propagation simulations. Expand its capabilities to include the **generation and offshore propagation** of **acoustic** and **tsunami** waves triggered by seismic faulting.
- ◆ Apply the modified tool to the **simulation of the 2011 Tohoku-Oki earthquake and tsunami**.

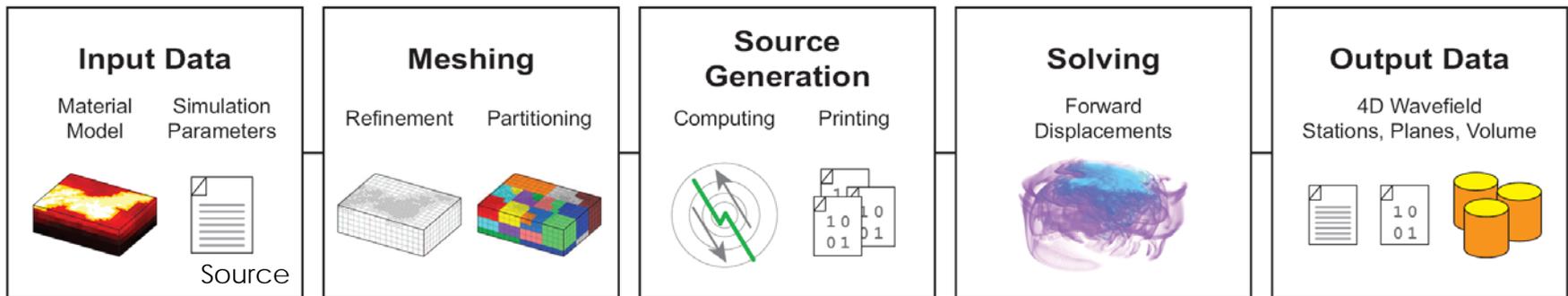
PART - I

COUPLING

EARTHQUAKE-TSUNAMI SIMULATIONS

Hercules

Our octree-based finite element tool for modeling earthquake ground motion* (Tu et al., SC2006)

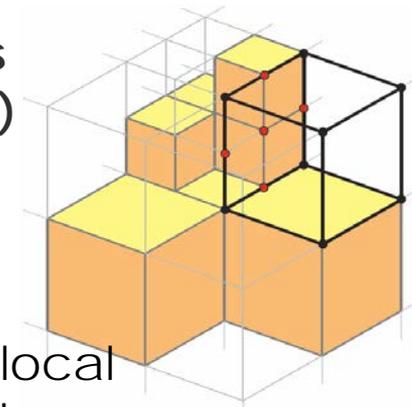


Hercules has been used for verification and validation studies (JB et al, GJI 2010; Taborda & JB, CiSE 2011, BSSA 2013,2014))

- TeraShake (2005–2007) SCEC
- ShakeOut (2007–2009) SCEC+USGS
- Chino Hills (2008–2013) SCEC
- Volvi (2008–2010) Euroseis E2VP

Octree-based FEM mesh

Mesh tailored to local shear wavelength



Berger, Young et al (1990s)

- and inventories of simplified building models (Isbiliroglu, Taborda & JB, Earthq. Spectra 2015)

Methodology

- ◆ We have chosen a **Multi-System Approach**

$$\ddot{p} - c_s^2 p_{,ii} = 0 \quad (1)$$

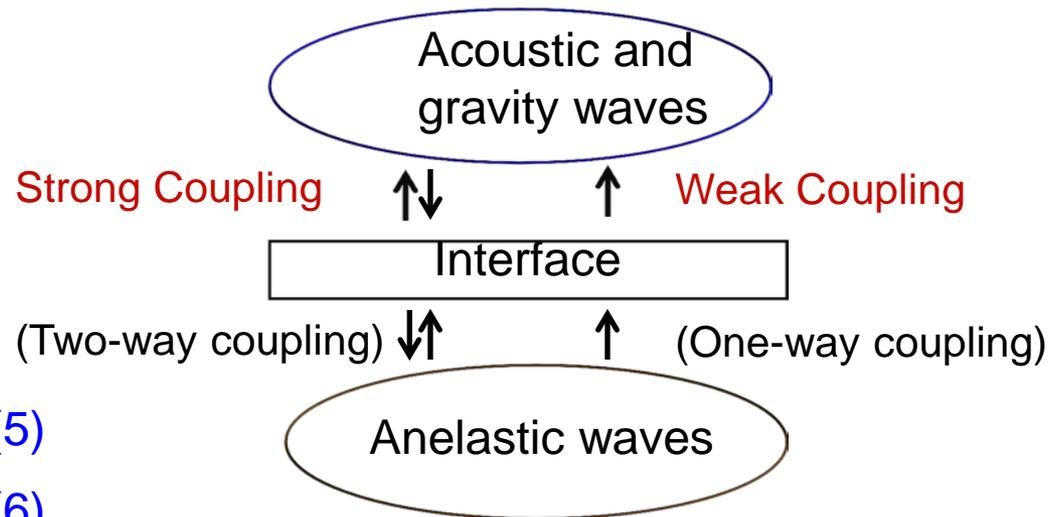
$$\frac{1}{g} \ddot{p} + p_{,i} n_i = 0 \quad \text{FS} \quad (2)$$

$$p_{,i}^A n_i^A - \rho^A \ddot{u}_i n_i^E = 0 \quad (3)$$

$$\sigma_{ij}^E n_j^E + p^A n_i^A = 0 \quad (4)$$

$$\rho_E \ddot{u}_i - \sigma_{ij,j} + f_i^B = 0 \quad (5)$$

$$\sigma_{ij} = \lambda u_{k,k} \delta_{ij} + \mu (u_{i,j} + u_{j,i}) \quad (6)$$



- ◆ **Numerical Discretization** (Applying standard Galerkin Method)

$$\mathbf{M}_{dd} \ddot{\mathbf{d}} + \mathbf{K}_{\kappa} \mathbf{d} + \mathbf{K}_{\mu} \mathbf{d} - \mathbf{R} \mathbf{p}^I = \mathbf{f}_d \quad (7) \quad \text{Solid Anelastic Domain}$$

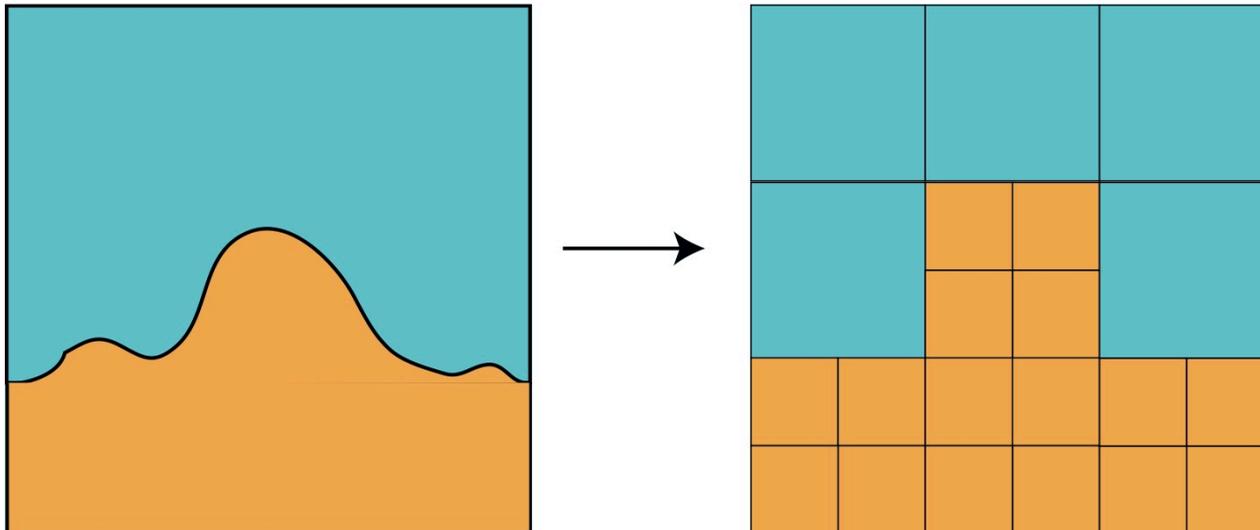
$$\mathbf{M}_{pp} \ddot{\mathbf{p}} + \mathbf{S} \mathbf{d}^I + \mathbf{K}_{pp} \mathbf{p} = \mathbf{f}_p \quad (8) \quad \text{Acoustic Domain}$$

- ◆ Requires a **new solution scheme** with additional **message passing** at the interface and appropriate computation schemes.

Interface Representation

DETECTION OF INTERFACE

- ◆ Detect bathymetry from **seismic velocity model** (no additional input).
- ◆ Acoustic domain in seismic velocity model is **assigned zero shear wave velocity**.
- ◆ Approximate the sea-solid interface region using **cubes**. (Same element scheme as for solid interfaces).

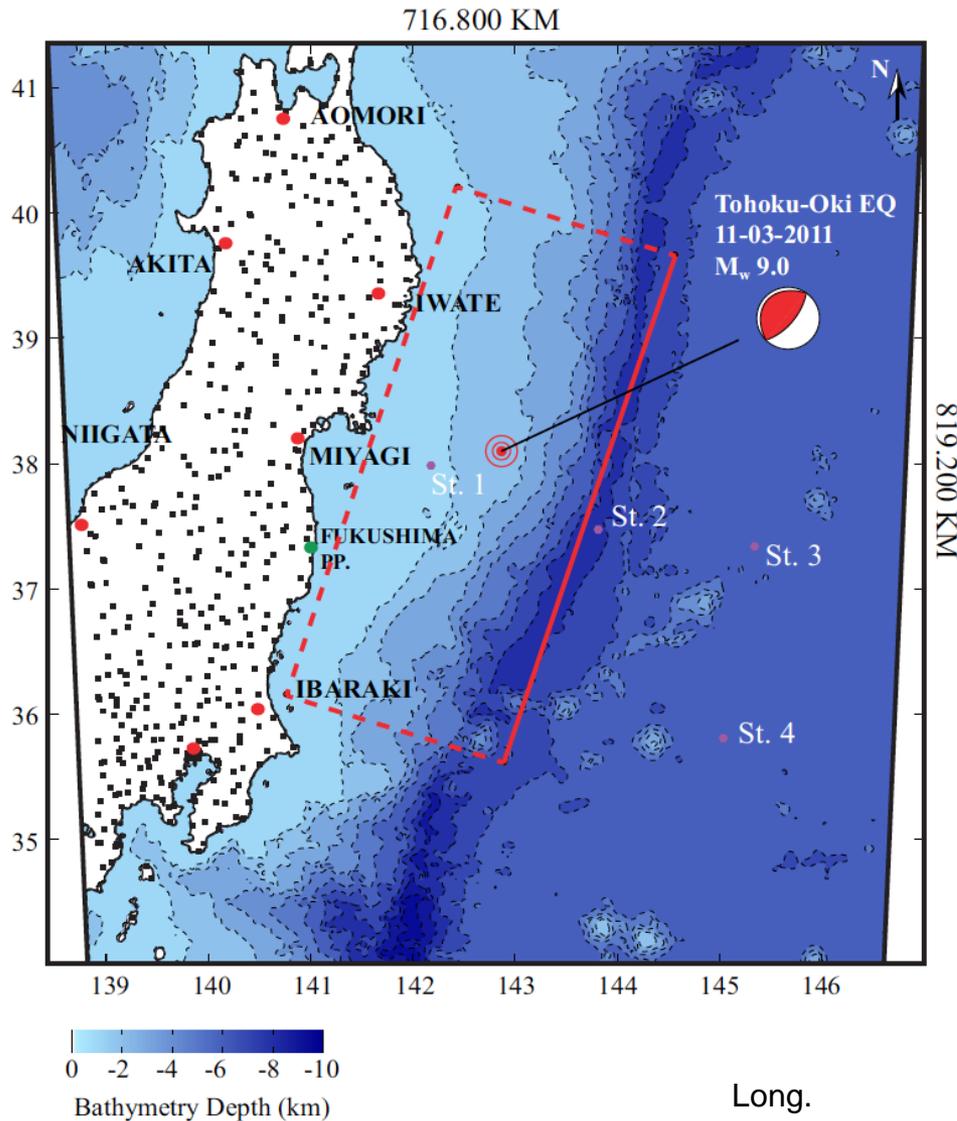


PART - II

2011 TOHOKU-OKI EARTHQUAKE AND TSUNAMI (3D)

Case Study

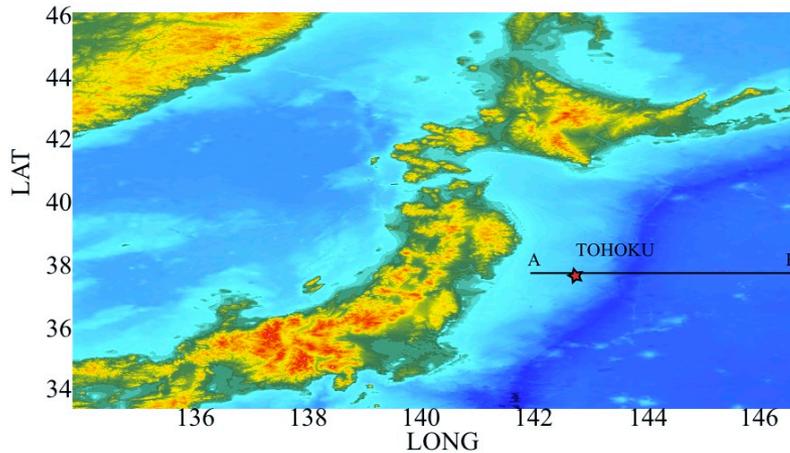
2011 Tohoku-Oki Earthquake and Tsunami



- ◆ A megathrust, subduction zone earthquake that generated tsunami waves.
- ◆ $M_w = 9.0$ – Fourth largest earthquake within the last 100 years.
- ◆ There are 467 stations in the region (K-net, Kik-net).

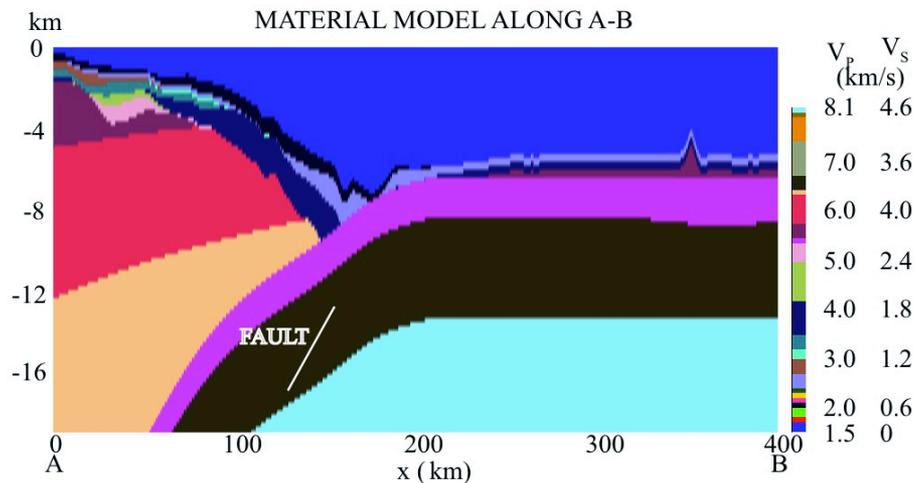
3D TOHOKU-OKI SIMULATION

NORTH-EASTERN JAPAN ELEVATION PROFILE

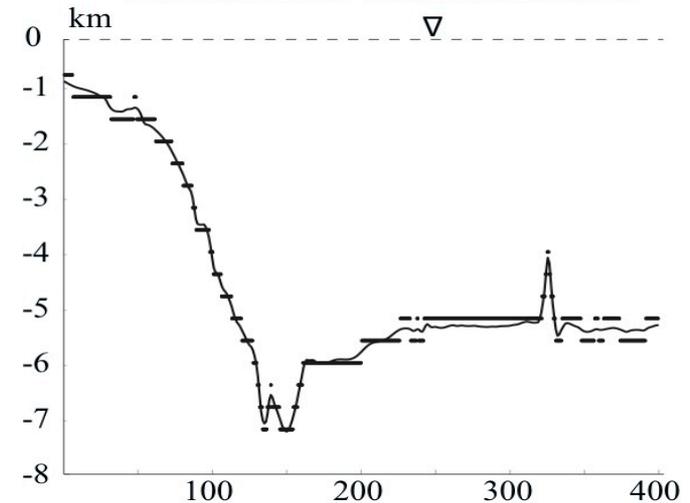


◆ Tsunami waves were observed predominantly in the E-W direction.

◆ 2D Cross-Section is taken along A-B (subduction zone) .



BATHYMETRY DISCRETIZATION

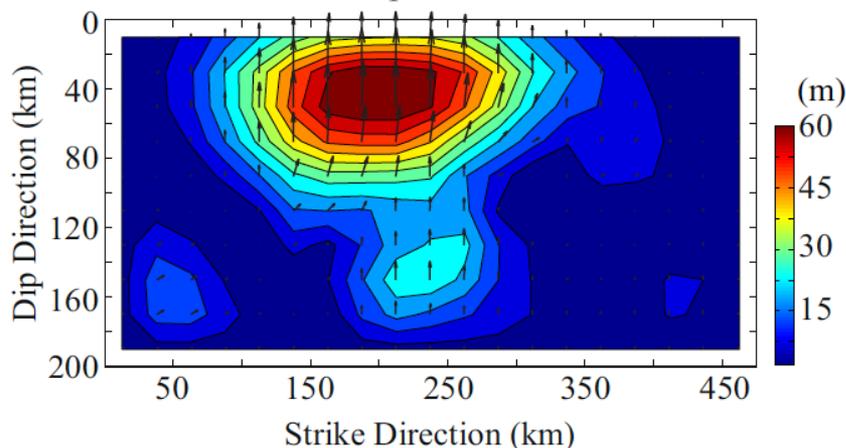


Notice horizontal and vertical scales are different

Case Study – 2011 Tohoku-Oki Earthquake

Source Model

Total Slip Distribution



◆ Source model by [Shao et. al. \(2011\)](#)

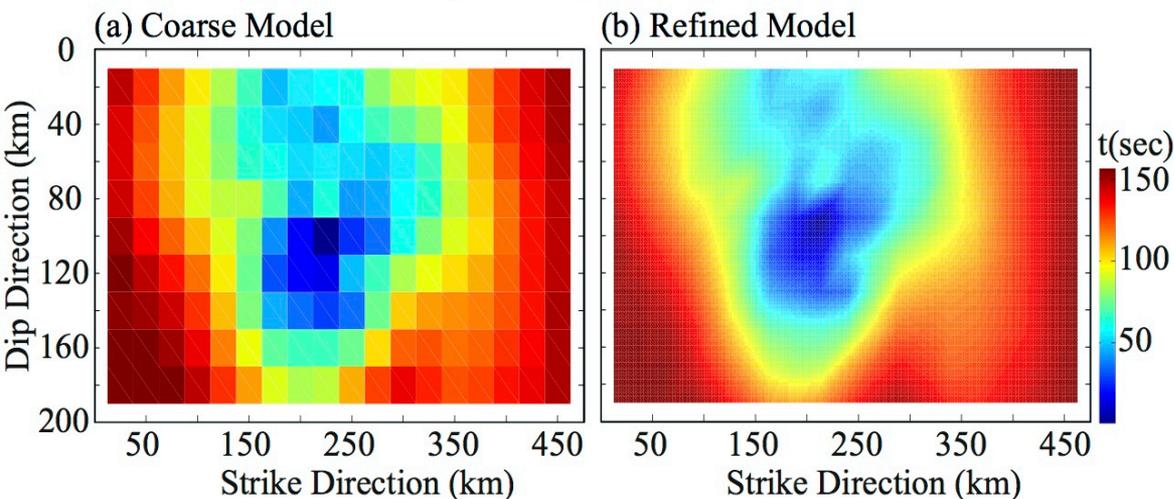
◆ **Smoothen** rupture initiation time using triangular prism shape functions.

◆ Multiple asperity rupture.

◆ First ruptures down dip.

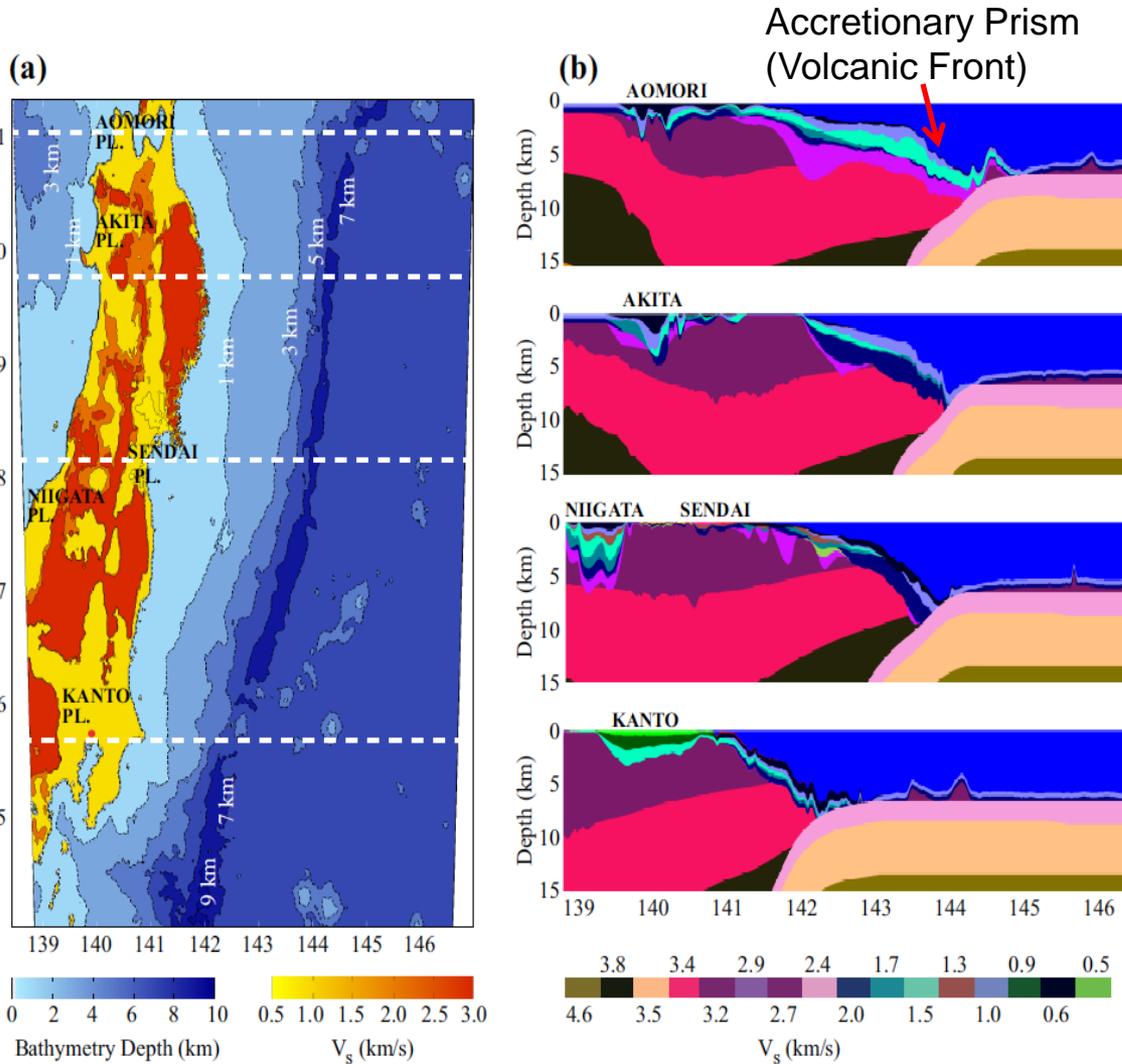
◆ Second ruptures up-dip (max. slip occurs here with 60 m)

Rupture Initiation Time



Case Study – 2011 Tohoku-Oki Earthquake

Seismic Velocity Model



- ◆ Velocity model in Long-Period Ground Motion Hazard Map report (2012) by NIED is used for the simulations.

- ◆ Computational area covers several sedimentary basins in Honshu.

- ◆ Aomori, Akita, Niigata and Kanto basins are deep but Sendai is a shallow one.

- ◆ The figure on the left shows the S-wave velocity distribution on the surface and bathymetry depth.

- ◆ The figure on the right shows the cross-sectional views of S-wave velocity distribution along the dashed lines.

Case Study – 2011 Tohoku-Oki Earthquake Simulations

SIMULATION PARAMETERS

Domain	
Length	819.2 km
Width	716.8 km
Depth	204.8 km
Temporal Resolution	
Simulation Δt	0.0045 s
Simulation time	1400 s
Number of steps	288,889
Spatial Resolution	
Maximum frequency	0.5 Hz
Minimum V_S	500 m/s
Points per wavelength	$8 \leq p < 16$
Minimum element size	100 m
Maximum element size	400 m
Number of elements*	686,508,844
Number of nodes	5,971,885,216
Number of dangling nodes	373,688,580

*The elements counted are triquadratic.

COMPUTATIONAL PERFORMANCE

		hh:mm:ss	%
Number of cores	19,200		
Elements per core	35,756		
Total wall clock	78,321 s	21:45:20	100.0
Meshing	311 s	5:11	0.4
Source Generation	17,122 s	04:45:22	22
Solving	60,694 s	16:51:34	77
Compute	44,398 s	12:19:58	57
I/O transactions	654 s	10:54	1
Communication	15,624 s	4:20:24	19
Service Units (SUs)	417,600		

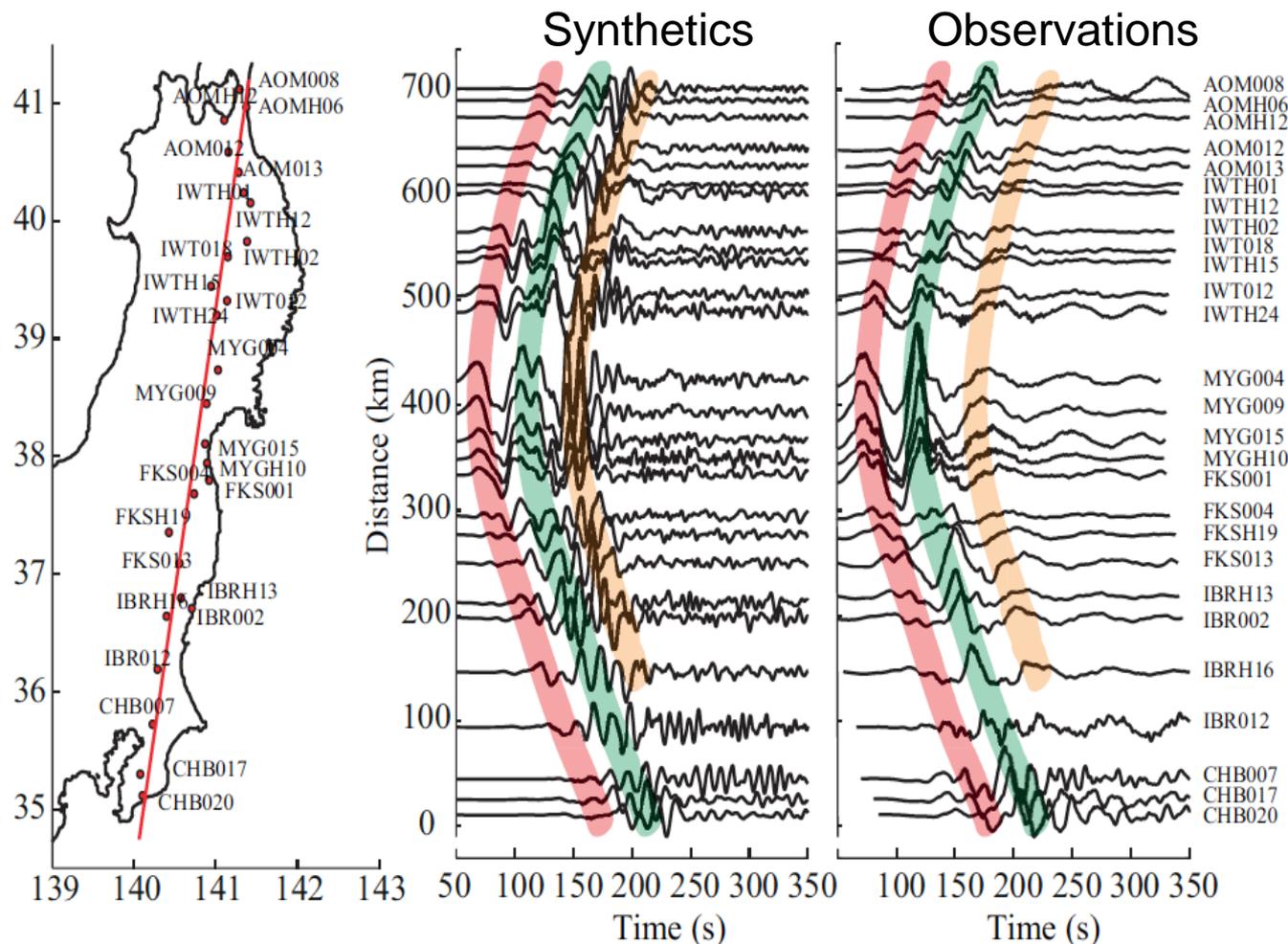
- Simulations conducted on [Blue Waters](#) (a petascale supercomputer).
- No significant difference** observed in the computational performance of strongly and weakly coupled simulations.

STRONG GROUND MOTION QUALITATIVE COMPARISON

Qualitative Validation – Seismic Ground Motion

On-Shore Station Records

Displacement Time Histories (East-West)
 Period range of 2-65 s



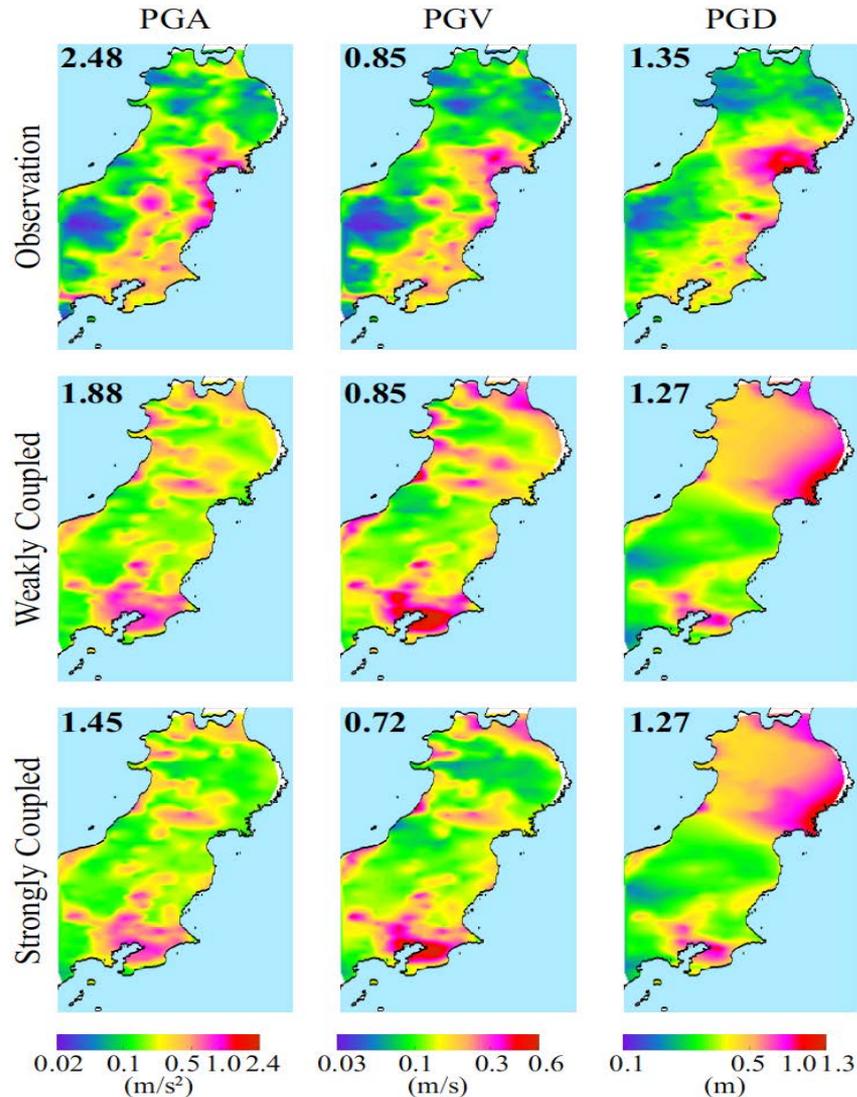
◆ Stations on a line extending from Aomori to Chiba prefecture (parallel to the strike direction of the fault).

◆ Synthetics capture the first two phases (direct waves).

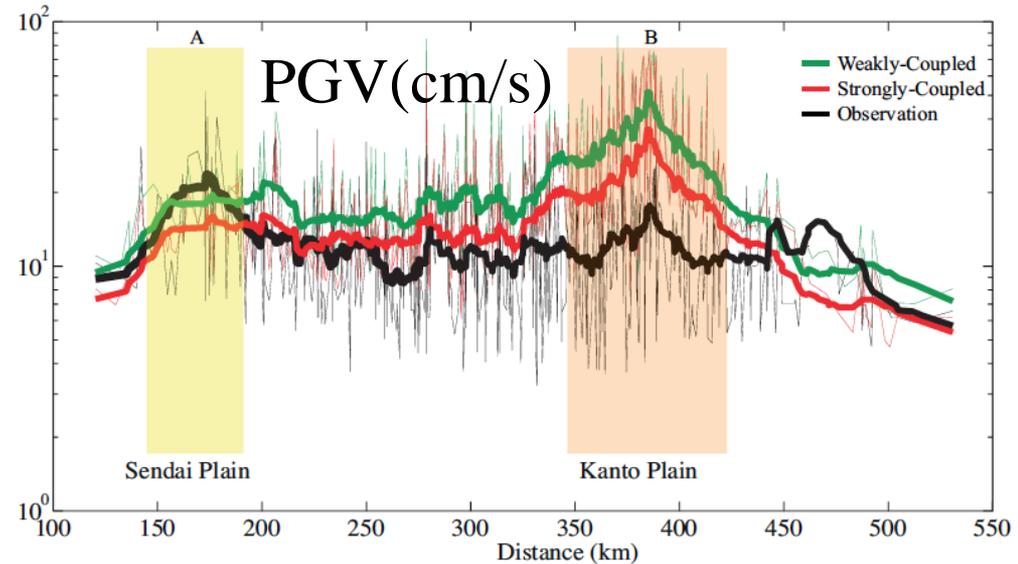
◆ Third phase and the prolonged ground motion in the Kanto basin is overestimated.

Qualitative Validation

Intensity Measures (Peak Ground Motion)

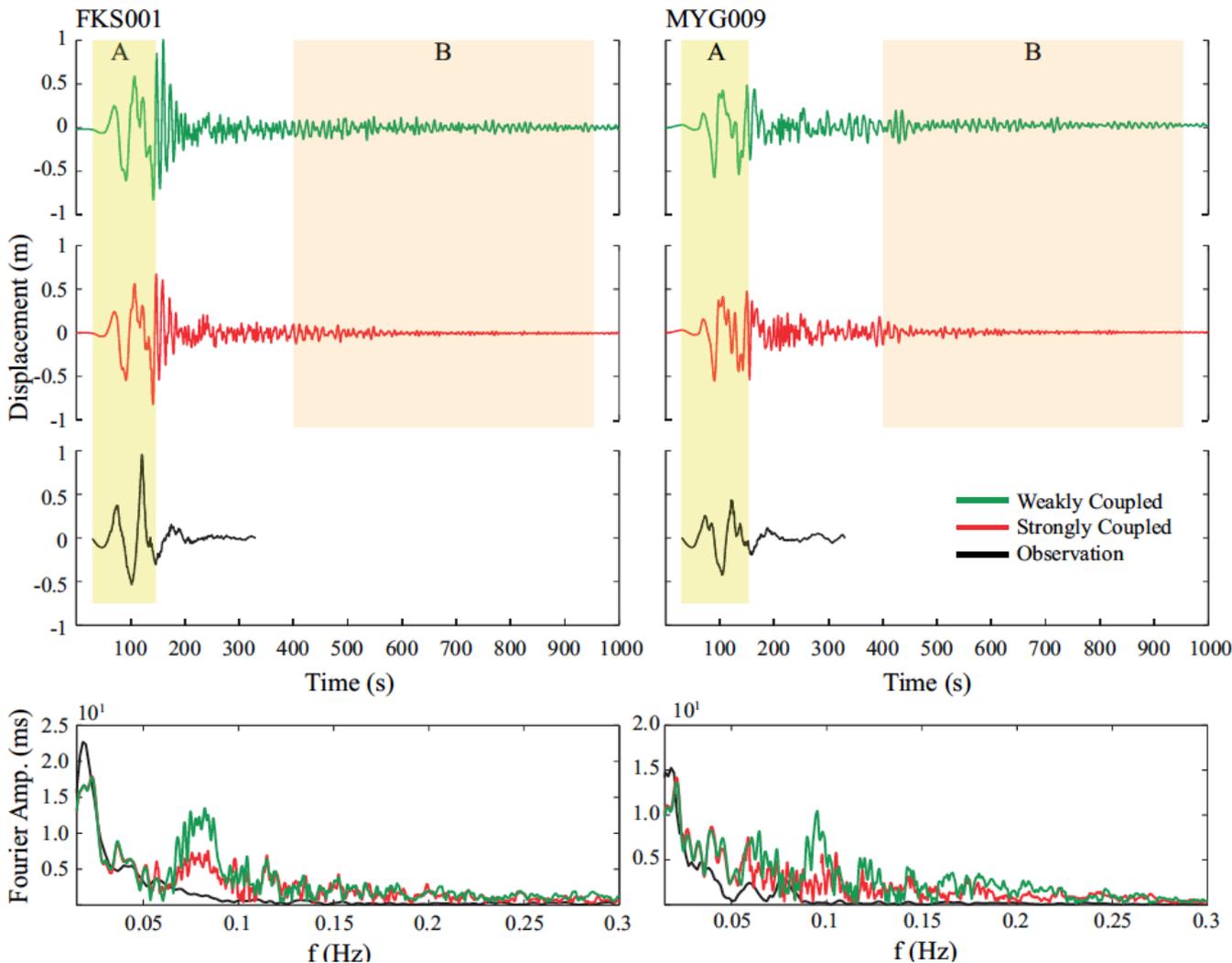


Seismic Attenuation Pattern



- ◆ PGV is overestimated especially in the Tohoku region and the Kanto basin.
- ◆ Introducing oceanic water layer reduces the misfit between the synthetics and the observations.

Qualitative Comparison Strongly Coupled vs Weakly Coupled

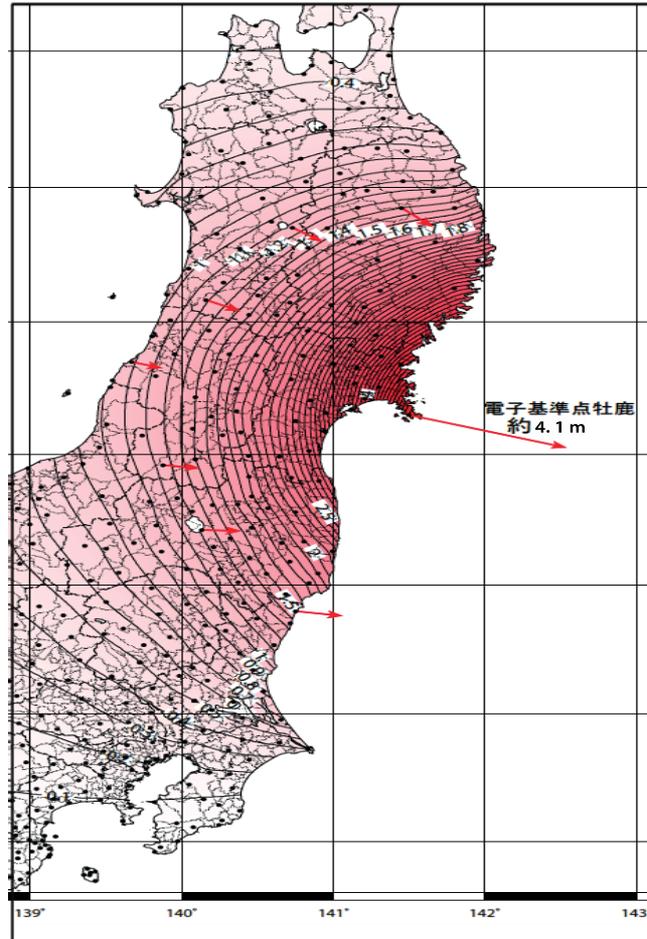
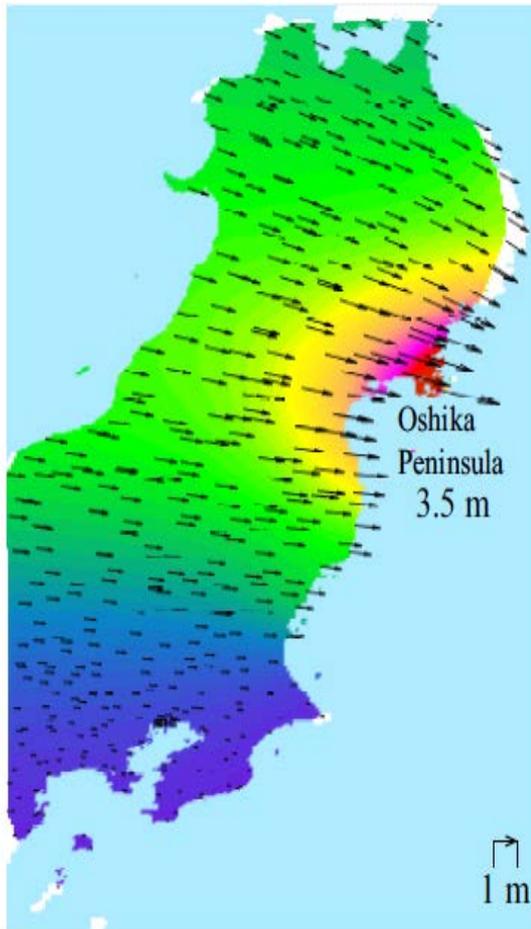


◆ (A) **Direct waves** are captured with almost no difference. The waves from the deep fault show a better fit.

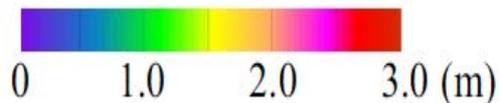
◆ (B) Strongly coupled case lowers the amplitude and ground motion duration. (**Absorbing effect of oceanic water layer**)

Quantitative Validation

Residual Displacement - Horizontal



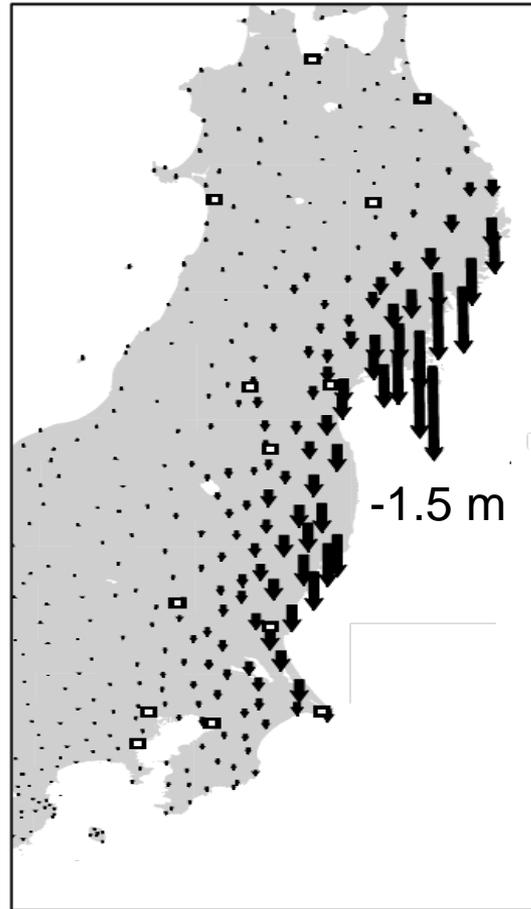
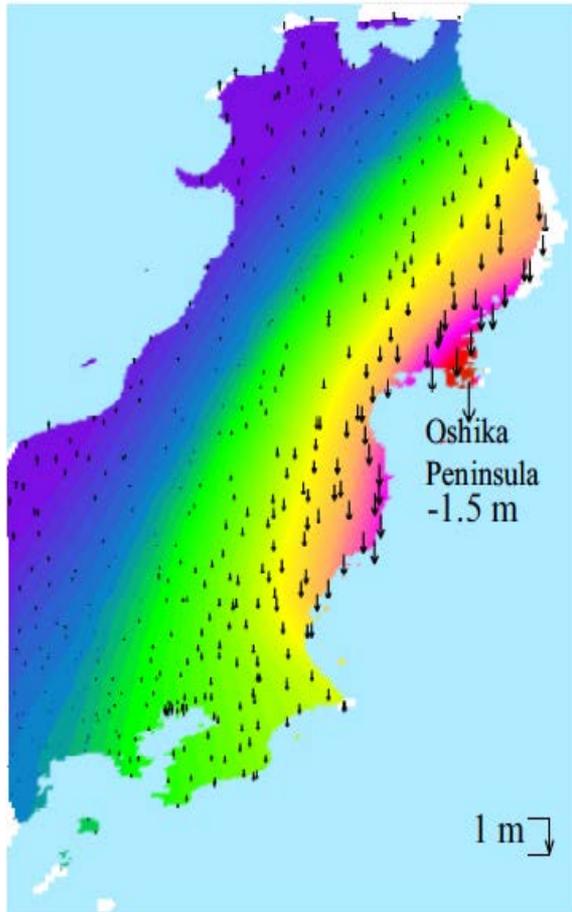
- ◆ From GPS station records, maximum horizontal deformation is observed on Oshika Peninsula.
- ◆ Overall distribution is captured with some underestimation.



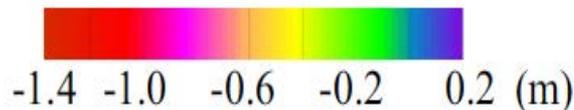
After JMA (2013)

Quantitative Validation

Residual Deformation - Vertical



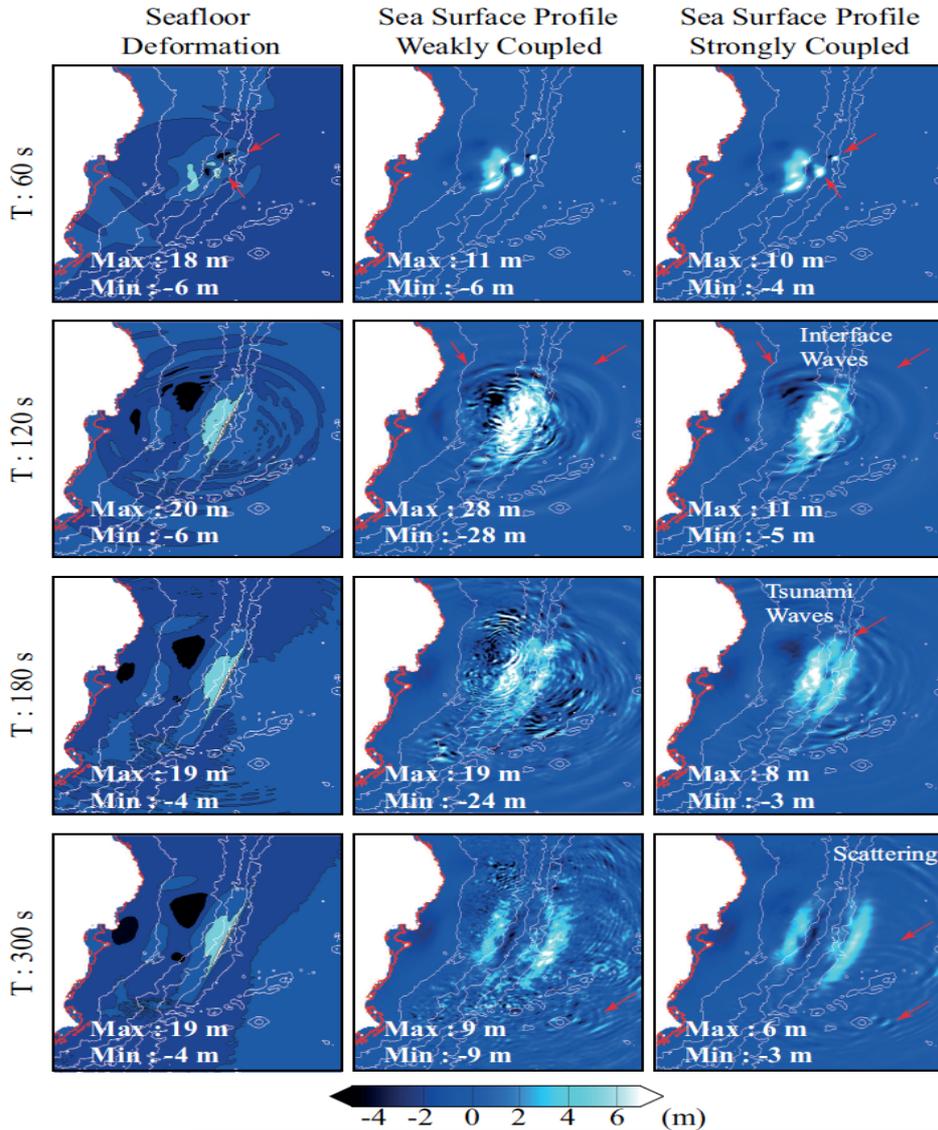
- ◆ From GPS station records, maximum vertical deformation is observed on Oshika Peninsula.
- ◆ Overall distribution is captured.



After Hashimoto (2013)

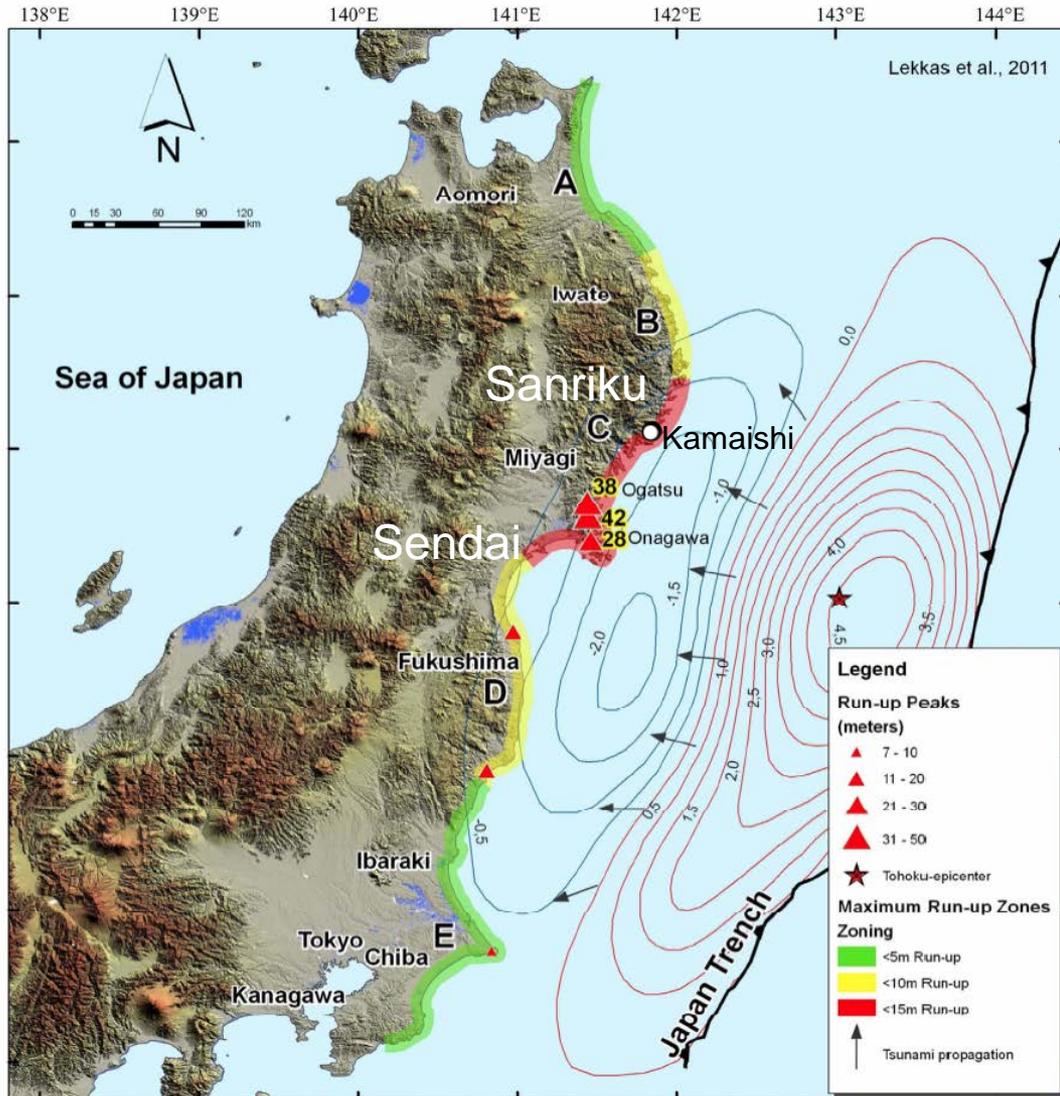
TSUNAMI WAVES

Qualitative Comparison Tsunami Generation



- ◆ Sea surface deformation is quite different from the tsunami waves profile.
- ◆ First tsunami waves are seen after 3 min (180 s).
- ◆ Sea surface waves accompanying interface waves are captured (early warning purposes)
- ◆ Weak coupling overestimates **acoustic fluctuations**.

Qualitative Comparison Tsunami Offshore Propagation

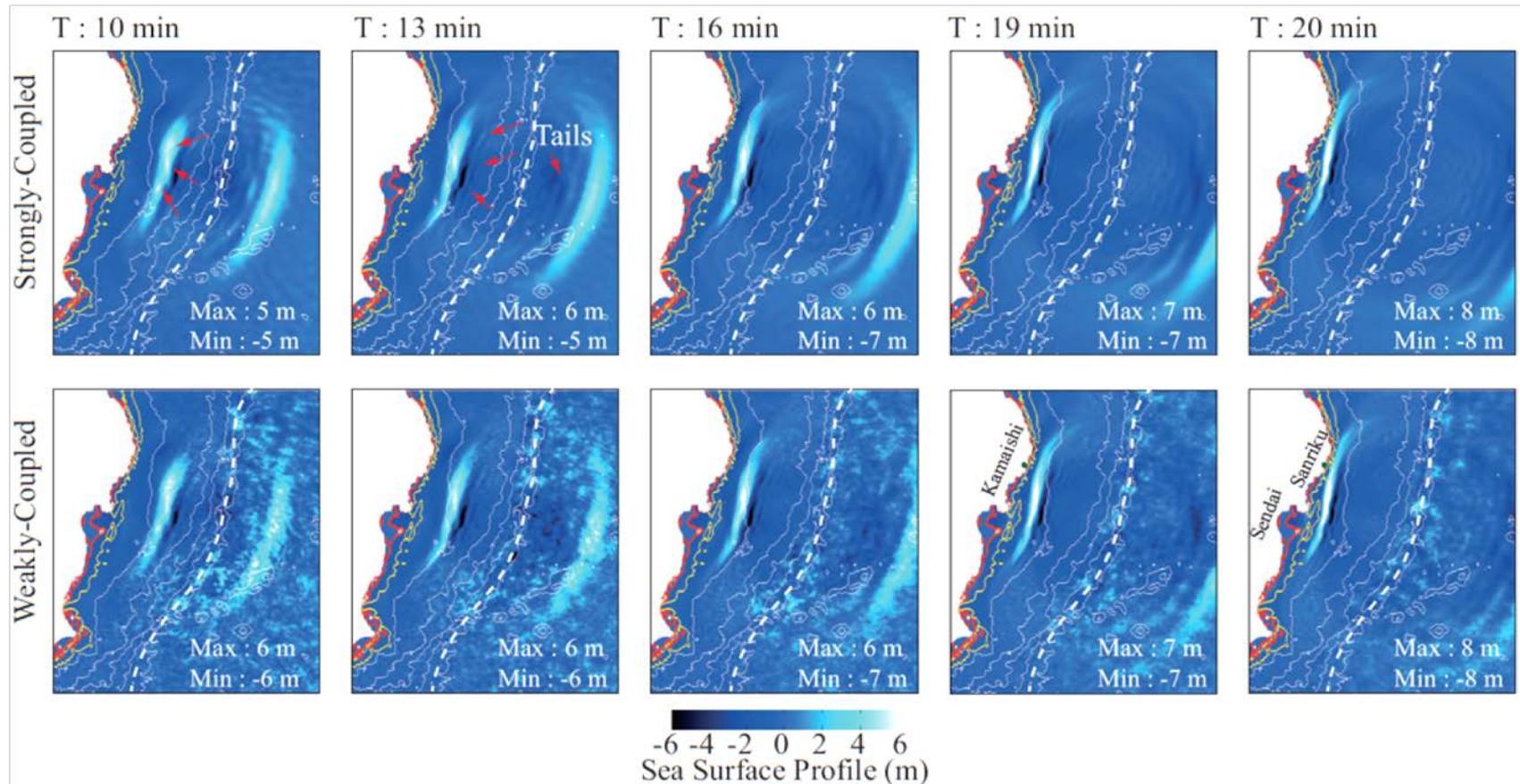


◆ Sendai and Sanriku coastlines were hit most by tsunami waves.

◆ First tsunami waves were observed around the city of Kamaishi.

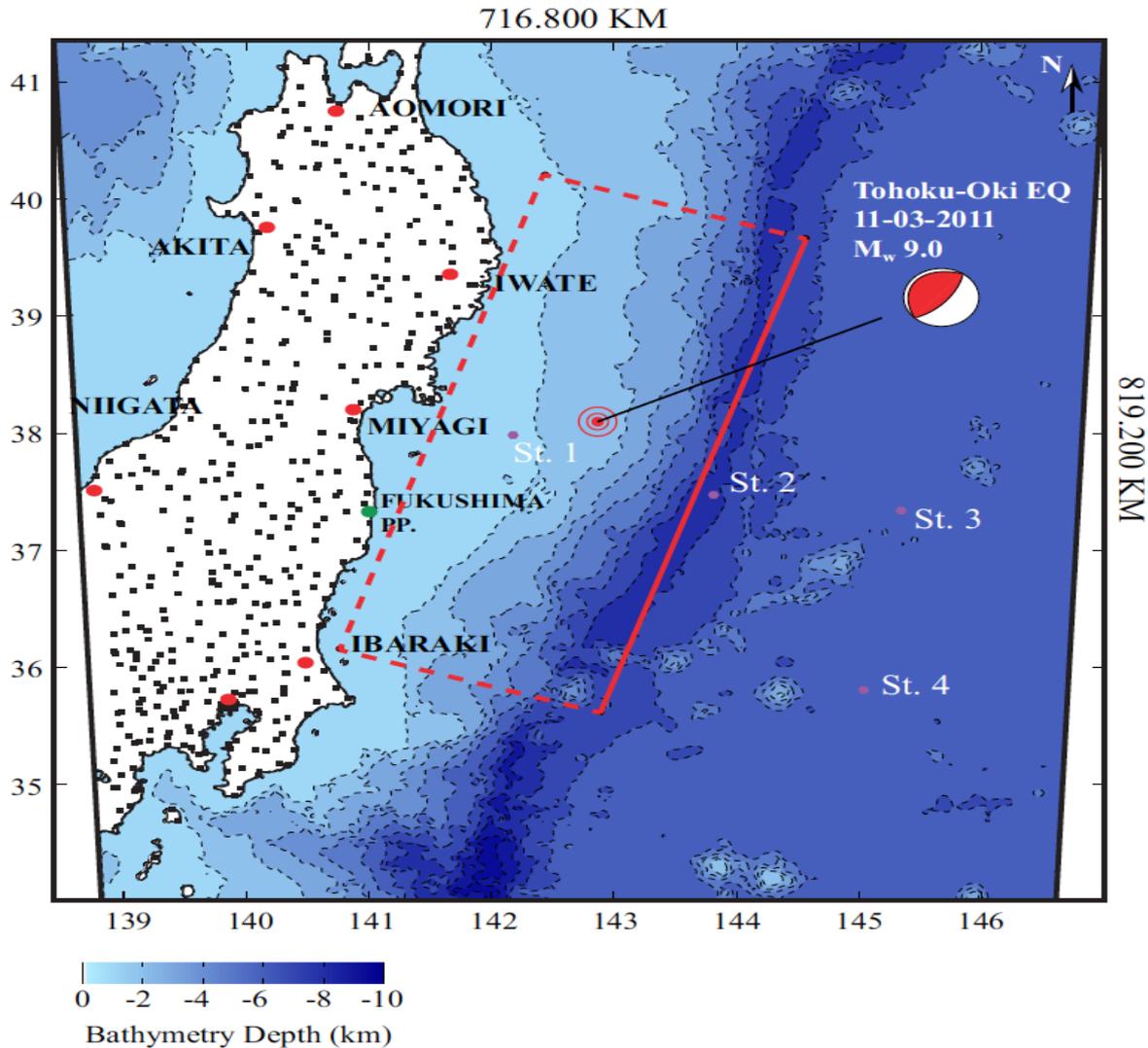
After [Lekkas et. al. \(2011\)](#)

Qualitative Comparison Tsunami Offshore Propagation



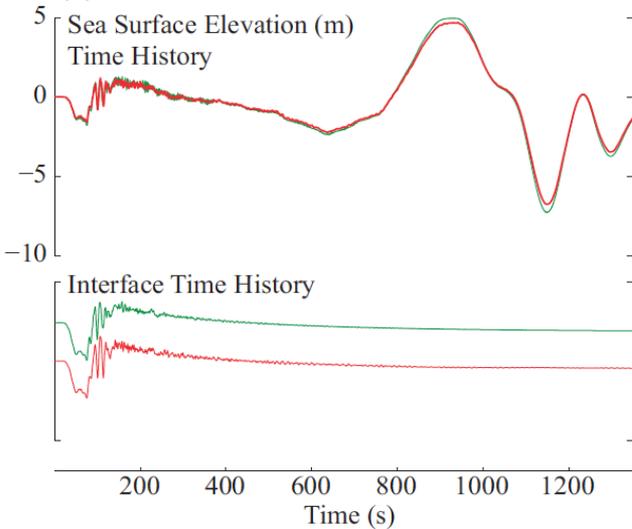
- ◆ To the west, tsunami waves heights increase and wavelengths decrease.
- ◆ Wave speed decreases as water depth decreases.

Sea Surface Elevation Stations

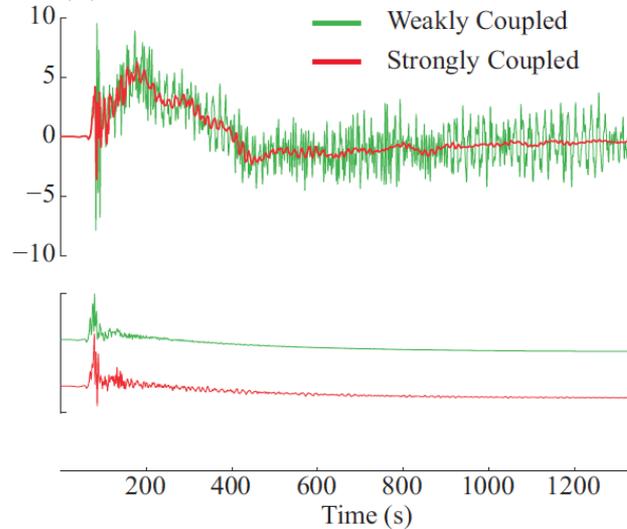


Qualitative Comparison Synthetics on Sea Surface

(a) St. 1



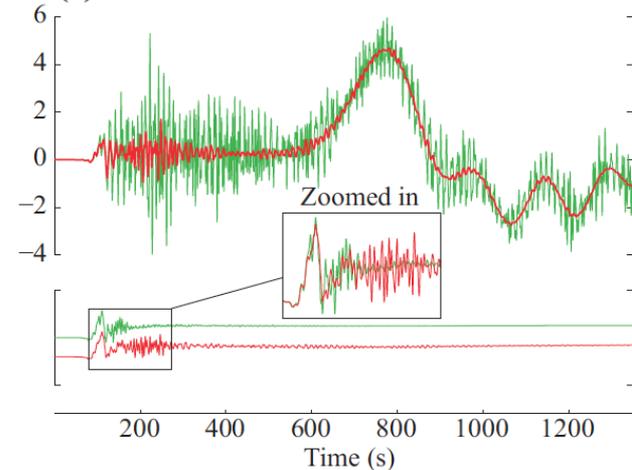
(b) St. 2



◆ Direct waves and interface waves are accompanied by identical sea surface elevation.

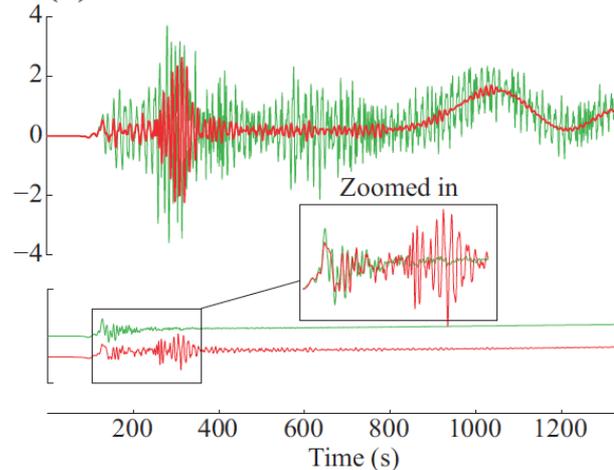
◆ Acoustic waves cannot travel upslope.

(c) St. 3



◆ Strong coupling leads to variation in the seafloor deformation histories (St. 3 and St. 4).

(d) St. 4



Case Study – 2011 Tohoku-Oki Earthquake

Conclusions

- ◆ Earthquake/tsunami simulation captures qualitatively and in some domains quantitatively the main characteristics of the ground motion and tsunami waves.
- ◆ Oceanic water layer has a **strong absorbing effect** on the surface waves, reducing the amplitude and duration significantly.
- ◆ Seismic attenuation patterns point to the **poor modeling of the Q** (Damping) in the material model especially in the **accretionary forearcs**.
- ◆ One-way coupling leads to an **overestimation of the acoustic waves**.

The End

Thank you

Anil, I wish you all the best always.