Empirical Uses of the Ground Rupture Database Glenn Biasi, University of Nevada Reno \* What can we say about the average rupture shape based on available rupture profiles?

\* Notes on the use of triangular shapes

\* Capturing rupture variability across all published ruptures

\* p(d | M) and p(M | d)

## Rupture Shape for an Unknown Earthquake

- \* Is there an average rupture shape?
- \* Does the average shape depend on rupture length?
- \* Use data set of rupture profiles from Wesnousky (2008)
- \* Subset selected of 24 with length >10 km

## Rupture Profile Data (1)









tosya AD: 2.51 m

## Rupture Profile Data (2)









- Challenge: how to combine ruptures of different lengths and displacements.
  - Combine using the method in Hemphill-Haley and Weldon (1999) – normalize by average displacement and length
  - \* Assume variability of displacements around mean is similar for large and small events.
  - \* Compare reversed and not reversed



## Mean, 24 Ruptures



#### Four ruptures <30 km



#### Five ruptures >200 km



## Notes on the Average Rupture Shape

- Including the reflected rupture shapes in effect doubles the data set under the expectation that next events will be similar to past ones.
- Normalizing by d<sub>ave</sub> removes most of the variability due to stress drop.
  - \* If you know the  $d_{ave}$  of the next rupture, use it.

# Would I be ahead to assume a triangular rupture profile?



Example: 90 km rupture, d<sub>max</sub>=6 m, d<sub>ave</sub> = 2.5 m Black: Left triangle Blue: Right triangle, reflection of left triangle Red: Average of both Cases:

(1)Assume left triangle, next rupture is left triangle. Mean error: 0

(2) Assume left triangle, next rupture is right triangle. Mean error 1.25 m.

(3) Assume mean, get either triangle: Mean error 0.625 m (about half)

(4) Assume mean, get nontriangle: Mean error <0.625 m

Conclusion: If you know the shape of the next rupture, use it. If not, use the mean rupture shape.

#### Other Uses of the Normalized Rupture

Profiles



Variability averaged

The variability of rupture displacement can be represented by an empirical probability density function.

 Make a histogram of d<sub>obs</sub>/d<sub>ave</sub> using all events -> p(d)



#### Probability of the d<sub>obs</sub> as a Function of Magnitude



using your favorite M-> d<sub>ave</sub> relationship -> p(d<sub>obs</sub> | M)



#### Probability of Magnitude Given a Displacement Observation



- Gather probabilities for all magnitudes considered and renormalize.

-Result is  $p(M | d_{obs})$ , the probability of an earthquake magnitude given one observation of displacement,  $d_{obs}$ .

-One can do better if more information is available. E.g. a prior distribution of earthquake magnitudes, an M<sub>max</sub>, or a probability of ground rupture vs. magnitude.

# **Concluding Remarks**

- The robustness of the average rupture shape suggests some constancy in mechanical behavior among faults.
  - sqrt(sin(x/2L)) works pretty well as an average rupture shape
- Normalizing by length and average displacement flattens differences in stress drop
  - \*  $M_o = mu^*L^*W^*d_{ave}$
  - \* If the stress drop of the next earthquake is known, it can be used to improve estimates.
- Under moderate assumptions rupture displacement variability from all documented ruptures can be encapsulated and used. E.g.,

\*  $p(d_{obs} | M)$  and  $p(M | d_{obs})$