### PFDHA

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Workshop on Surface Fault Displacement Hazard UC Berkeley, May 21, 2009 A Methodology for Probabilistic Fault Displacement Hazard Analysis

- Initially developed to assess fault rupture hazard for the proposed Yucca Mountain nuclear waste repository
- Refined in hazard study for Los Alamos
- Published in *Earthquake Spectra*, v. 19
- Methodology has general applicability
- Probability distributions developed for only normal faulting earthquakes

## **Two Approaches**

- Earthquake Approach
  - Uses PSHA formulation
  - Considers two types of faulting
    - Principal faulting slip on the main plane of weakness responsible for the release of seismic energy during earthquake
    - *Distributed* faulting slip on other faults, fractures or shears in the vicinity of the principal rupture
- Displacement Approach
  - Uses the characteristics of fault displacement observed at the site of interest without invoking a specific mechanism for their cause

#### Principal and Distributed Faulting



### Earthquake Approach Formulation

• PSHA

$$v_k(z) = \sum_n \alpha_n(m^0) \int_{m^0}^{m_n^u} f_n(m) \left[ \int_0^\infty f_n(r|m, \text{Site } k) \cdot P(Z > z|m, r) \right] dr dm$$

• PFDHA

$$v_k(d) = \sum_n \alpha_n(m^0) \int_{m^0}^{m_n^u} f_n(m) \left[ \int_0^\infty f_n(r|m, \text{Site } k) \cdot P^*(D > d|m, r, \text{Site } k) \, dr \right] \cdot dm$$

## Fault Displacement "Attenuation" Function

 $P_n^*(D > d | m, r, \text{Site } k) = P_n(\text{Slip}|m, r) \cdot P_{kn}(D > d | m, r, \text{Site } k, \text{Slip})$ 

*P<sub>n</sub>*(Slip|*m,r*) probability that (surface) slip occurs given the event

*P<sub>n</sub>(D>d|m,r,Site k, Slip)* probability distribution for the amount of slip give some slip occurs

## $P_n(Slip|m,r)$ for Principal Rupture

- Can be developed by randomly locating ruptures on fault plane as in standard PSHA calculation
- Alternatively, use empirical models for probability of surface rupture as a function of magnitude
  - Data needed is yes/no for occurrence of surface rupture in event of magnitude M



#### $P_n(D>d|m,r,Site k, Slip)$ for Principal Rupture

- Assess D<sub>average</sub> or D<sub>max</sub> as a function of magnitude from empirical models (e.g. Wells and Coppersmith, 1994)
- Develop probability distribution for a normalized displacement D/D<sub>average</sub> or D/D<sub>max</sub>
  - Account for location of site along the length of the rupture
  - Data needed is detailed mapping of amount of displacement along the length of the rupture

#### Displacement Variability Along Rupture Length



#### Example $P_n(D > d | m, r, \text{Site } k, \text{Slip})$





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## $P_n(Slip|m,r)$ for Distributed Rupture

- Data needed is detailed mapping of distributed ruptures around the feature of main interest to geologists
- Map density of distributed ruptures for historical events
- Subdivide area into pixels (0.5 km x 0.5 km)
- Probability (frequency) of distributed rupture is equal to number of pixels with distributed rupture divided by total number of pixels
- Tradeoff between pixel size and completeness of mapping



## $P_n(Slip|m,r)$ for Distributed Rupture

 Model probability of rupture a as function of distance from principal rupture, hanging wall versus foot wall, and magnitude



#### $P_n(D>d|m,r,Site k, Slip)$ for Distributed Rupture

- Data needed is the amplitude of displacement on the secondary ruptures
- Very limited amount of data reported
- Modeled as displacement normalized by principal fault displacement



# Displacement Approach $v(d) = \lambda_{DE} \cdot P(D > d | \text{Slip})$

- $\lambda_{DE}$  is frequency of displacement events
  - Number of events in time period T
  - Slip rate divided by average displacement per event
  - Average displacement computed from observations at site or from relationships between scale (e.g. length) of feature and displacement  $\overline{D} \alpha' I$ 
    - $\overline{D}_E = \alpha' L_{Total}$
  - Data needed is characterization of specific feature at site of interest

# P(D>d|Slip)

 Developed from data for normalized distributions of displacement in individual slip events



## **Displacement Hazard Curves**

- Different shape than ground motion hazard curves due to effect of probability of slip (smaller earthquakes unlikely to produce surface rupture
- Integral of hazard curve provides an estimate of fault slip rate that provides a check on consistency of modeling

